

Causality in Economics and Econometrics
An Entry for the *New Palgrave Dictionary of Economics*

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Abstract
of
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An entry for the *New Palgrave Dictionary of Economics*. Traces the history of causality in economics and econometrics since David Hume. Examines the main modern approaches to causal inference.

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Causality in Economics and Econometrics

1. Philosophers of Economics and Causality

The full title of Adam Smith's great foundational work, *An Inquiry into the Nature and Causes of the Wealth of Nation* (1776), illustrates the centrality of causality to economics.

The connection between causality and economics predates Smith. Starting with Aristotle, the great economists are frequently also the great philosophers of causality. Aristotle's contributions to economics are found principally in the *Topics*, the *Politics*, and the *Nicomachean Ethics*, while he lays out his famous four causes (material, formal, final, and efficient) in the *Physics*. Material and formal causes are among the concerns of economic ontology, a subject addressed by philosophers of economics (see e.g., Mäki 2001) albeit rarely by practicing economists. Sometimes, as for example in Karl Marx's grand theory of capitalist development, economists have appealed to final causes or teleological explanation (for a defense, see Cohen 1978; for a general discussion, see Kincaid 1996). But for the most part, taking physical sciences as a model, causal modeling in economics deals with efficient causes: What is it that makes things happen? What explains change? (See Bunge 1963 for a broad account of the history and philosophy of causal analysis.)

The greatest of the philosopher/economists, David Hume, set the tone for much of the later development of causality in economics. On the one hand, economists inherited from Hume the sense that practical economics was essentially a causal science. In "On Interest," Hume (1742, p. 304) writes:

it is of consequence to know the principle whence any phenomenon arises, and to distinguish between a cause and a concomitant effect. Besides that the speculation is curious, it may frequently be of use in the conduct of public affairs. At least, it

must be owned, that nothing can be of more use than to improve, by practice, the method of reasoning on these subjects, which of all others are the most important; though they are commonly treated in the loosest and most careless manner.

On the other hand, Hume doubted whether we could ever know the essential nature of causation “in the objects” (Hume 1739, p. 165). Coupled with a formidable critique of inductive inference more generally, Hume’s skepticism has contributed to a wariness about causal analysis in many sciences, including economics (Hume 1739, 1777). The tension between the epistemological status of causal relations and their role in practical policy runs through the history of economic analysis since Hume.

2. History

2.1 HUME’S FOUNDATIONAL ANALYSIS

Although Hume was an economist and historian, physical illustrations serve as his paradigm causal relationships. *A* (say, a billiard ball) strikes *B* (another ball) and causes it to move. Any analysis must address two key features of causality: First, causes are asymmetrical (in general, if *A* causes *B*, *B* does not cause *A*). Hume sees temporal succession (the movement of *A* precedes the movement of *B*) as accounting for asymmetry. Second, causes are effective. A cause must be distinguished from an accidental correlation and must bring about its effect. Hume sees spatial contiguity (the balls touch) and necessary connection (the movement of *B* follows of necessity from the movement of *A*) as distinguishing causes from accidents and establishing their effectiveness.

Hume was famously skeptical of any idea that could not be traced either to logical or mathematical deduction or to direct sense experience. Hume asks, whence comes the idea of the necessary connection of cause and effect? It cannot be deduced from first

principles. So, he argues that our idea of necessary connection, which he concedes is the most characteristic element of causality, can arise only from our experience of the constant conjunction of particular temporal sequences. But this then implies that causality stands on a very weak foundation. For one corollary of Hume's belief that all ideas are based either in logic or sense experience was that we do not have any secure warrant for inductive inference. Neither logic nor experience (unless we beg the question by implicitly assuming the truth of induction) gives us secure grounds from observing instances to inferring a general rule. Therefore, what we regard as necessary connection in causal inference is really more of habit of mind without clear warrant. Causes may be necessarily connected to effects; but, for Hume, we shall never know in what that necessary connection consists.

While later philosophers have differed with Hume on the analysis of causality, his views were instrumental in setting the agenda, not only for philosophical discussions but for practical causal analysis as well.

2.2 THE NINETEENTH CENTURY: LOGIC AND STATISTICS

Even more influential than Hume in shaping economics, John Stuart Mill, another philosopher/economist, was less skeptical about causal inference in general, but more skeptical about its application to economics. In his *System of Logic* (1851), Mill advanced his famous canons of induction: the methods of (i) agreement, (ii) difference, (iii) joint (or double) agreement and difference, (iv) residues, and (v) concomitant variations. For example, according to the method of difference, if we have two sets of circumstances, one in which a phenomenon occurs and one in which it does not, and the circumstances agree in all but one respect, that respect is the cause of the phenomenon.

Mill's canons are essentially abstractions from the manner in which causes are inferred in controlled experiments. As such, Mill doubted that the canons could be easily applied to social or economic situations, in which a wide variety of uncontrolled factors are obviously relevant. Mill argued in his *Principles of Political Economy* (1848) that economics was an "inexact and separate science," whose general principles were essentially known *a priori* and which held only subject to *ceteris paribus* clauses (see Hausman 1992). Mill's apriorism proved to be hugely influential in later economics. Lionel Robbins (1935) and the Austrian economists, such as Mises (1966), took it to the extreme, denying that economics could be an empirical discipline. It also influenced those economists who see economic theory as similar to physical theory as a domain of universal laws.

Other 19th century economists were less skeptical about the application of causal reasoning to economic data. For instance, W. Stanley Jevons (1863) pioneered the construction of index numbers as the core element of an attempt to prove the causal connection between inflation and the increase in world-wide gold stocks after 1849. Jevon's investigation can be interpreted as an application of Mill's method of residues (see Hoover and Dowell 2001). He saw the various idiosyncratic relative price movements owing to supply and demand for particular commodities as canceling out to leave the common factor that could only be the effect of changes in the money stock.

The 19th century witnessed extensive development in the theory and practice of statistics (Stigler 1986). Inference based on statistical distributions and correlation measures were closely connected to causality. Adolphe Quetelet envisaged the inferential problem in statistics as one of distinguishing among constant, variable, and

accidental causes (Stigler 1999, p. 52). The economist Francis Ysidro Edgeworth pioneered tests of statistical significance (in fact Edgeworth may have been the first to use this phrase). He glossed the finding of a statistically significant result as one that “comes by cause” (Edgeworth 1885, pp. 187-188).

2.3 THE TWENTIETH CENTURY: CAUSALITY AND IDENTIFICATION

Further developments of statistical techniques, such as multiple correlation and regression, in the 20th century were frequently associated with causal inference. It was fairly quickly understood that, unlike correlation, regression has a natural direction: the regression of Y on X does not produce coefficient estimates that are the algebraic inverse of those from the regression of X on Y . The direction of regression should respect the direction of causation.

By the early 20th century, however, the dominant vision of economics – equally for advocates of partial equilibrium analysis, such as Marshall (1930), as for advocates of general equilibrium analysis, such as Walras (1954) – was one in which prices and quantities are determined simultaneously. Simultaneity does not necessarily rule out causal order, though it does complicate causal inference. Although regressions may have a natural causal direction, there is nothing in the data on their own that reveal which direction is the correct – each is an equally eligible rescaling of a symmetrical and noncausal correlation. This is a problem of observational equivalence. And it is the obverse side of the now familiar problem of econometric identification: in this case, how can we distinguish a supply curve from a demand curve? The problem of identification was pursued through most of the first half of the 20th century until the fairly complete treatment by the Cowles Commission at mid-century (Koopmans 1950; Hood and

Koopmans 1953; see Morgan 1990 for a thorough treatment of the history of the identification problem).

The standard solution to the identification problem is to look for additional causal determinants that discriminate between otherwise simultaneous relationships. Both the supply of milk and demand for milk depend on its own price. If, however, the supply also depends on the price of alfalfa used to feed the cows and the demand also on the daily high temperature (which affects the demand for milk to make ice cream), then supply and demand curves can be identified separately. Identification can be viewed through the glasses of simultaneous equations, pushing causality into the background, or it can be viewed as a problem in causal articulation. In the first case, economists frequently use the language of exogenous variables (the price of alfalfa; the temperature) and endogenous variables (the price and quantity of milk). Exogenous variables can also be regarded as the causes of the endogenous variables. From the 1920s to the 1950s, different economists placed different emphasis on the causal aspects of identification (Morgan (1990) and the various papers reprinted in Hendry and Morgan (1995)).

Modern econometrics can be dated from the development of structural econometric models following the pioneering work in the 1930s of Jan Tinbergen, the conceptual foundations of probabilistic econometrics in Trygve Haavelmo's (1944) "Probability Approach to Econometrics," and the technical elaboration of the identification problem in the two Cowles Commission volumes. Structural models did not in themselves necessarily favor the language of identification over the language of causality. Indeed, in Tinbergen's (1951) textbook, dynamic, structural models are explicated with a diagram that uses arrows to indicate causal connections among time-

dated variables. Nevertheless, after the econometric work of the Cowles Commission, two approaches can be clearly distinguished.

One approach, associated with Hermann Wold and known as *process analysis*, emphasized the asymmetry of causality, typically grounded it in Hume's criterion of temporal precedence (Morgan 1991). Wold's process analysis belongs to the time-series tradition that ultimately produced Granger causality and the vector autoregression (see Section 3 below).

The other approach, associated with the Cowles Commission, related causality to the invariance properties of the structural econometric model. This approach emphasized the distinction between endogenous and exogenous variables and the identification and estimation of structural parameters. Implicitly, structural modelers accepted Mill's *a priori* approach to economics. While they differed from Mill in their willingness to conduct empirical investigations, the selection of exogenous (or *instrumental*) variables was seen to be the province of *a priori* economic theory – a maintained assumption rather than something to be learned from data itself. In his contribution to the Cowles Commission volume, Herbert Simon (1953) showed that causality could be defined in a structural econometric model not only between exogenous and endogenous variables, but also among the endogenous variables themselves. And he showed that the conditions for a well-defined causal order are equivalent to the well-known conditions for identification. Despite the equivalence, with the demise of process analysis and the ascendancy of structural econometrics – aided indirectly perhaps by a revival of Humean causal skepticism among logical positivist philosophers of science – causal language in economics virtually collapsed between 1950 and about 1990 (Hoover 2004).

3. Alternative Approaches to Causality in Economics

Different approaches to causality can be classified along two lines as in Table 1. On the one hand, approaches may emphasize structure or process. On the other hand, approaches may rely on *a priori* identifying assumptions or they may seek to infer causes from data. The upper left cell, the *a priori* structural approach, represented by the Cowles Commission, dominated economics for most of the postwar period. But since we already discussed it at some length in Section 2 and since it was largely responsible for turning the economics profession away from *explicit* causal analysis, we add nothing more about it here and instead turn to the other cells in Table 1.

3.1 THE INFERENTIAL STRUCTURAL APPROACH

The most important of the inferential structural approaches is due to Simon (1953).

Simon eschews temporal order as a basis for causal asymmetry and, instead, looks to recursive structure. As we observed in Section 2, Simon's account is closely related to the Cowles Commission structural approach. Consider the bivariate system:

$$(1) \quad Y_t = \theta X_t + \varepsilon_{1t},$$

$$(2) \quad X_t = \varepsilon_{2t},$$

where the random error terms ε_{it} are independent, identically distributed and θ is a parameter. Simon says that X_t causes Y_t , because X_t is recursively ordered ahead of Y_t . One knows all about X_t without knowing about Y_t , but one must know the value of X_t to

determine the value of Y_t . Equations (1) and (2) also appear to show that any intervention in (2), say a change in the variance of ε_{2t} , would transmit to (1); while any intervention in (1), say a change in θ or the variance of ε_{1t} , would not transmit to (2). Apparently, X_t could then be used to control Y_t .

Unfortunately, merely being able to write an accurate description of the two variables in the form of (1) and (2) does not guarantee either the apparent asymmetry of information or control. Consider the following related system:

$$(3) \quad Y_t = \omega_{1t},$$

$$(4) \quad X_t = \delta Y_t + \omega_{2t},$$

where $\delta = \frac{\theta \text{var}(\varepsilon_2)}{\theta^2 \text{var}(\varepsilon_2) + \text{var}(\varepsilon_1)}$, $\omega_{1t} = \varepsilon_{1t} + \theta \varepsilon_{2t}$, and $\omega_{2t} = (1 - \delta \theta) \varepsilon_{2t} - \delta \varepsilon_{1t}$. It is easy to

show that ω_{1t} and ω_{2t} are uncorrelated; so that (3) and (4) have a form analogous to (1) and (2) with the causal roles reversed. Apparently, Y_t causes X_t on Simon's criterion, even though (3) and (4) have exactly the same likelihood function (i.e., the same reduced form) and so describe the data equally well. While it looks like the key parameters for (3) and (4) are derived from those of (1) and (2), we could have taken (3) and (4) as the starting point and derived (1) and (2) symmetrically. What we would like to do is to replace the equal signs with arrows that show that the causal direction runs from the right-hand to the left-hand sides in the regression equations in one of the systems, but not in the other. Unfortunately, there is no way to do this, no choosing between the systems,

on the basis of a single set of data by itself. This is the problem of observational equivalence again.

The *a priori* Cowles Commission approach relies on economic theory to provide appropriate identifying assumptions to resolve the observational equivalence. Sims (1980) attacked the typical application of the Cowles Commission approach to structural macroeconometric models as relying on “incredible” identifying assumptions: economic theory was simply not informative enough to do the job. But Simon, who was otherwise supportive of the conception of causality in the Cowles Commission took a different tack.

Simon sees the problem as choosing between two alternative sets of parameters: which set contains the structural parameters, $\{\theta$ and the variances of the $\varepsilon_{it}\}$ or $\{\delta$ and the variances of the $\omega_{it}\}$? Simon suggested that experiments – either controlled or natural – could help to decide. If, for example, an experiment could alter the conditional distribution of X_t without altering the marginal distribution of Y_t , then it must be that Y_t causes X_t , because this would be possible only if a structure like (3) and (4) characterized the data. If it did, a change in the conditional distribution would involve either δ or the variance of ω_{2t} , neither of which would affect the variance of ω_{1t} . In contrast, if (1) and (2) truly characterized the causal structure of the data, a change to the conditional distribution of X_t would, in fact, involve a change to the variance of ε_{2t} , which, according to the equivalences above, would alter either δ or the variance of ω_{2t} . Similar relationships of stability and instability in the face of changes to the marginal distribution can also be demonstrated (Hoover 2001, chapter 7). The appeal to experimental evidence is what marks Simon’s approach out as inferential rather than *a priori*.

Hoover (1990, 2001) generalizes Simon's approach to the type of nonlinear systems of equations found in modern rational-expectations models. He shows that Simon's idea of natural experiments can be operationalized by coordinating historical, institutional, or other non-statistical information with information from structural break tests on what, in effect, amounts to the four regressions corresponding to (1)-(4) above generalized to include lagged dynamics. With allowances for complications introduced by rational expectations, the key idea is that, in the true causal order, interventions that alter the parameters governing the true marginal distribution do not transmit forward to the conditional distribution (characterized by (1) or (4)) nor do interventions in the true conditional distribution transmit backward to the marginal distribution (characterized by (2) or (3)). Since the true structural parameters are not known *a priori*, non-statistical information is important in identifying an intervention as belonging to the process governing one variable or another.

Although avoiding the term "causality," Favero and Hendry (1992) analysis of the Lucas critique in terms of "superexogeneity" is also a variant on Simon's causal analysis (Ericsson and Irons 1995; Hoover 2001, chapter 7). Superexogeneity is essentially an invariance concept (Engle, Hendry, and Richard 1983). Favero and Hendry find evidence against the Lucas critique (noninvariance in the face of policy regime changes) in the superexogeneity of conditional probability distributions in the face of structural breaks in marginal distributions – the same sort of evidence that Hoover cites as helping to identify causal direction.

The recent revival of causal analysis in microeconomics in the guise of "natural experiments," although apparently developed independently of Simon, nonetheless

proceeds in much the same spirit as Hoover's version of Simon's approach (Angrist and Krueger 1999, 2001). This literature typically employs the language of instrumental variables. A natural experiment is a change in a policy or a relevant environmental factor that can be identified non-statistically. Packaged as an econometric instrument, the experiment can be used – in much the same way that variations in alfalfa prices and temperature were used in the example in Section 2 – to identify the underlying relationships and to measure the causally relevant parameters.

3.2 THE INFERENTIAL PROCESS APPROACH

Perhaps the most influential explicit approach to causality in economics is due to Clive W. J. Granger (1969). Granger causality is an inferential approach, in that it is data-based without direct reference to background economic theory; and it is a process approach, in that it was developed to apply to dynamic time-series models (see Kuersteiner's entry "Granger Causality" in this dictionary for technical details). Granger-causality is an example of the modern probabilistic approach to causality, which is a natural successor to Hume (e.g., Suppes 1970). Where Hume required constant conjunction of cause and effect, probabilistic approaches are content to identify cause with a factor that raises the probability of the effect: A causes B if $P(B|A) > P(B)$, where the vertical "l" indicates "conditional on". The asymmetry of causality is secured by requiring the cause (A) to occur before the effect (B).¹

Granger's (1980) definition is more explicit about temporal dynamics than is the generic probabilistic account, and it is cast in terms of the incremental predictability of one variable conditional on another:

¹ The probability criterion is not enough on its own to produce asymmetry since $P(B|A) > P(B)$ implies $P(A|B) > P(A)$.

X_t Granger-causes Y_{t+1} if $P(Y_{t+1} | \text{all information dated } t \text{ and earlier})$
 $\neq P(Y_{t+1} | \text{all information dated } t \text{ and earlier omitting information about } X)$.

This definition is conceptual, as it is impracticable to condition on *all* past information.

In practice, Granger-causality tests are typically implemented through bivariate regressions:

$$(5) \quad Y_t = \Pi_{11}Y_{t-1} + \Pi_{12}X_{t-1} + v_{1t},$$

$$(6) \quad X_t = \Pi_{21}Y_{t-1} + \Pi_{22}X_{t-1} + v_{2t},$$

where the Π_{ij} are parameters, and the v_{it} are random error terms. In practice, lag lengths may be larger than one, but far less than the infinity implicit in the general definition. X_t Granger-causes Y_{t+1} if $\Pi_{12} \neq 0$, and Y_t Granger-causes X_{t+1} if $\Pi_{21} \neq 0$.

Christopher Sims (1972) famously used Granger-causality to demonstrate the causal priority of money over nominal income. Later, as part of a generalized critique of structural econometric models, Sims (1980) advocated vector autoregressions (VARs) – atheoretical time-series regressions analogous to equations (1) and (2), but generally including more variables with lagged values of each appearing in each equation. In the VAR context, Granger-causality generalizes to the multivariate case.

While Granger-causality has something useful to say about incremental predictability, there is no close mapping between Granger-causality and structural notions

of causality on either the Cowles Commission or Simon's accounts (Jacobs, Leamer, and Ward 1979). Consider a structural model:

$$(7) \quad Y_t = \theta X_t + \beta_{11} Y_{t-1} + \beta_{12} X_{t-1} + \varepsilon_{1t},$$

$$(8) \quad X_t = \gamma Y_t + \beta_{21} Y_{t-1} + \beta_{22} X_{t-1} + \varepsilon_{2t},$$

where ε_{1t} and ε_{2t} are identically distributed, independent random errors and θ , γ and the β_{ij} s are structural parameters. The independence of the parameters and the error terms implies that causality runs from the right-hand to the left-hand sides of each equation.

Equations (5) and (6) can be seen as the reduced forms of (7) and (8).

We focus on X causing Y . X structurally-causes Y if either θ or $\beta_{12} \neq 0$. And X Granger-causes Y if $\Pi_{12} = \frac{\beta_{12} + \theta\beta_{22}}{1 - \theta\gamma} \neq 0$. Thus, if X Granger-causes Y , then X

structurally causes Y . Note, however, that this result is particular to the case in which (7) and (8) represents the universe, so that (5) and (6) represent the complete conditioning on past histories of relevant variables. If the universe is more complex and the estimated VAR does not capture the true reduced forms of the structural system, which in practice they may not, then the strong connection suggested here does not follow.

More interestingly, even if (5)-(8) are complete, structural causality does not necessarily imply Granger-causality. Suppose that $\beta_{12} = \beta_{22} = 0$, but $\theta \neq 0$, then X structurally causes Y , but since $\Pi_{12} = 0$, X does not Granger-cause Y .

Now suppose that X does not Granger-cause Y . It does not necessarily follow that X does not structurally cause Y , since if θ , β_{12} , and $\beta_{22} \neq 0$, and $-\beta_{12}/\beta_{22} = \theta$, then it will still be true that $\Pi_{12} = 0$. This may appear to be an odd special case, but in fact

conditions such as $-\beta_{12}/\beta_{22} = \theta$ arise commonly in optimal control problems in economics.

A simple physical example makes it clear what is happening. Suppose that X measures the direction of the rudder on a ship and Y the direction of the ship. The ship is pummeled by heavy seas. If the helmsman is able to steer on a straight course, effectively moving the rudder to exactly cancel the shocks from the waves, the direction of the rudder (in ignorance of the true values of the shocks) will not predict the course of the ship. The rudder would be structurally effective in causing the ship to turn, but it would not Granger-cause the ship's course.

3.3 THE *A PRIORI* PROCESS APPROACH

The upper right-hand cell of Table 1 is represented by Arnold Zellner's (1979) account of causality (cf. Keuzenkamp 2000, chapter 4, section 4). Zellner's notion of causality is borrowed from the philosopher Herbert Feigl (1953, p. 408), who defines causation "... in terms of predictability according to law (or more adequately, according to a set of laws)." On the one hand, Zellner opposes Simon and sides with Granger: predictability is a central feature of causal attribution, which is why his is a process account. On the other hand, he opposes Granger and sides with Simon: an underlying structure (a set of laws) is a crucial presupposition of causal analysis, which is why his is an *a priori* account.

Much obviously depends on what a law is. Zellner's own view is that a law is a (probabilistic) description of a succession of states of the world that holds for many possible boundary conditions and covers many possible circumstances. He couches his position in an explicitly Bayesian theory of inference. Feigl identifies causality with

lawlikeness or predictability. It is the fact that formulae fit previously unexamined cases, as well as examined ones, that constitutes their lawlikeness. This is close to Simon's invariance criterion (the true causal order is the one that is invariant under the right sort of intervention).

The central problem, then, is how to distinguish laws from false generalizations or accidental regularities – that is, how to distinguish conditional relations invariant to interventions from regularities that are either not invariant or are altogether adventitious. Zellner believes that a theory serves as the basis for discriminating laws from casual generalizations. Although Zellner's approach permits us to learn some things from the data, in keeping with the spirit of Bayesian inference, it does so within a narrowly defined framework (cf. Savage's (1954, pp. 82-91) "small world" assumption). Economic theory in Zellner's account restricts the scope of an investigation *a priori*.

Zellner objects to Granger-causality for two reasons. First, it is not satisfactory to identify cause with temporal ordering, as temporal ordering is not the ordinary, scientific or philosophical foundation of the causal relationship. Second, Granger's approach is atheoretical. In order to implement it practically, an investigator must impose restrictions – limit the information set to a manageable number of variables, consider only a few moments of the probability distribution (in our exposition, just the mean), and so forth. For Zellner, if these restrictions cannot be explained theoretically, Granger's methods will discover only accidental regularities.

Zellner explicitly criticizes Granger for ignoring the need for theoretical basis for empirical investigation – implicitly focusing on only one side of a process in which theory informs empirics and empirics informs theory. He criticizes Simon for defining

cause to be a formal property of a model (recursive order) without making essential reference to empirical reality. Zellner's criticism is, however, more aptly directed at the Cowles Commission approach, since (as we saw in Section 3.1) Simon distinguishes himself through tying causal order to empirical inference.

3.4 STRUCTURAL VECTOR AUTOREGRESSIONS

Not all approaches to causality fall quite neatly into the cells of Table 1; or more to the point, an approach that falls into one cell may morph into one that falls into another cell. The history of Sims's VAR program is an important case.

Sims (1980) advocated VARs as a reaction to the manner in which the Cowles Commission program, which identified structural models through *a priori* theory, had been implemented (see Section 3.2). From a causal perspective, it was closely related to Granger's analysis. Starting with VAR such as equations (5) and (6), Sims wished to work out how various "shocks" would affect the variables of the system. This is complicated by the fact that the error terms in (5) and (6), which might be taken to represent the shocks, are not in general independent, so that a shock to one is a shock to both, depending on how correlated they are. Sims's initial solution was to impose an arbitrary orthogonalization of the shocks (a Choleski decomposition). In effect, this meant transforming (5) and (6) into a system like (6) and (7) and setting either θ or γ to zero. This amounts to imposing a recursive order on X_t and Y_t , such that the covariance matrix of the error terms is diagonal (i.e., ε_{1t} and ε_{2t} are uncorrelated). A shock to X can then be represented by a realization of ε_{1t} and a shock to Y by a realization of ε_{2t} .

Initially, Sims treated the choice of recursive order as a matter of indifference. Criticizing the VAR program from the point of view of structural models, Leamer (1985)

and Cooley and LeRoy (1985) pointed out that the substantive results (e.g., impulse-response functions and innovation accounts) depend on which recursive order is chosen. Sims (1982, 1986) accepted the point and henceforth advocated structural vector autoregressions (SVARs). SVARs can be identified through the contemporaneous causal order only. So, for example, to identify (5) and (6), it is enough to assume that either θ or γ in (7) or (8) is zero; one need not make any assumptions about the β_{ij} s. Ironically, since the initial impulse behind the VAR program was to avoid theoretically tenuous identifying assumptions, the choice of restrictions on contemporaneous variables used to transform the VAR into the SVAR are typically only weakly supported by economic theory.

Nevertheless, the move from the VAR to the SVAR is a move from an inferential to an *a priori* approach. It is also a move from a fully non-structural, process approach to a partially structural approach, since the structure of the contemporaneous variables, though not of the lagged variables, is fully specified. The SVAR approach can, therefore, be seen as straddling the cells on the first line of Table 1.

3.5 THE GRAPH-THEORETIC APPROACH TO CAUSAL INFERENCE

A final approach to causality in economics sometimes provides another example of an inferential structural approach, and sometimes straddles the cells on the second line of Table 1. Graph-theoretic approaches to causality were first developed outside of economics (Pearl 2000; Spirtes, Glymour, and Scheines 2000), but have recently been applied within economics (Swanson and Granger 1997, Akleman, Bessler, and Burton 1999; Bessler and Lee 2002; Demiralp and Hoover 2003).

The key ideas of the graph-theoretic approach are simple. (See Demiralp and Hoover (2003) or Hoover (2005) for a detailed discussion). Any structural model can be represented by a graph in which arrows indicate the causal order. Equations (1) and (2) are represented by $X \rightarrow Y$ and equations (3) and (4) by $Y \rightarrow X$. More complicated structures can be represented by more complicated graphs. Simultaneity, for instance, can be represented by double-headed arrows. The graphs allows us easily to see the dependence or independence among variables. Pearl (2000) and Sprites *et al.* (2000) demonstrate the isomorphism between causal graphs and the independence relationships encoded in probability distributions. This isomorphism allows conclusions about probability distributions to be derived from theorems proven using the mathematical techniques of graph theory.

Many of the results of graph-theoretic analysis are straightforward. Suppose that $A \rightarrow B \rightarrow C$ (that is, A causes B causes C). A and C would be probabilistically dependent, but conditional on B , they would be independent. Similarly for $A \leftarrow B \leftarrow C$. In each case, B is said to *screen* A from C . Suppose that $A \leftarrow B \rightarrow C$. Then, once again A and C would be dependent, but conditional on B , they would be independent. B is said to be the *common cause* of A and C . Now suppose that A and B are independent conditional on sets of variables that exclude C or its descendants, and $A \rightarrow C \leftarrow B$, and none of the variables that cause A or B directly causes C . Then, conditional on C , A and B are dependent. C is called an *unshielded collider* on the path ACB . (A *shielded* collider would have a direct link between A and B .) These are the simplest relationships of probabilistic dependence and independence. More complex ones may also obtain in

which A is independent of B only conditional on more than one other variable (say, C and D).

A number of causal search algorithms have been developed (Sprites *et al.* 2000). These start with information about correlations (or other tests of unconditional and conditional statistical independence) among variables. The most common of these, the PC algorithm, assumes that graphs are strictly recursive (known in the literature as *acyclical*) and starts with a graph in which all variables are causally connected with an unknown causal direction. It then tests for independence among pairs of variables, conditioning on sets of zero variables, then one, then two, and so forth until the set of variables is exhausted. Whenever it finds independence, it removes the causal connection between the variables in the graph. Once the graph is pared down as far as can be, it considers triples of variables in which two are conditionally independent but are connected through a third. If conditioning on that third variable renders the variables conditionally dependent, then that variable is unshielded collider and it is connected to the other two variables with causal arrows running toward it. After all the unshielded colliders have been identified, further logical analysis can be used to orient additional causal arrows. For example, we might reason as follows: suppose we have a triple $A \rightarrow C \text{ --- } B$; unless the causal arrow runs away from C toward B , C would be identified as an unshielded collider; but C was not identified as an unshielded collider earlier in the search; therefore, the causal arrow must run away from C toward B .

Sometimes the data allow the complete orientation of a causal graph, but sometimes some causal connections are left undirected. In this case, the graph marks out an equivalence class, and the algorithm has identified 2^n causal graphs consistent with the

empirical probability distribution, where n = the number of undirected causal connections.

While most applications of graph-theoretic methods assume that the true causal structures are recursive (i.e., strictly acyclical), economics frequently treats variables that are cyclical or simultaneously determined. Although the recursiveness assumption is restrictive, it is an assumption that is also frequently made in the SVAR literature. Some progress has been made in developing graph-theoretic search algorithms for cyclical or simultaneous causal systems (Pearl 2000, pp. 95-96, 142-143; Richardson 1996; Richardson and Spirtes 1999).

Swanson and Granger (1997) showed that estimates of the error terms of the VAR (the v_{it} in equations (5) and (6)) can be treated as the original time-series variables purged of their dynamics. A causal order identified on such variables corresponds to the causal order necessary to convert a VAR into an SVAR. Demiralp and Hoover (2003) present Monte Carlo evidence that the PC algorithm is effective at selecting the true causal connections among variables and, when signal strengths are high enough, moderately effective at directing them correctly. Search algorithms can, therefore, reduce or even eliminate the need to appeal to *a priori* theory when identifying the causal order of an SVAR.

Where Simon's approach looked for relatively important interventions as a basis for causal inference to a structure, the graph-theoretic approach uses relatively routine random variations to identify patterns of conditional independence that map out causal structures. The two approaches are complementary: Simon's approach may be used to

resolve the observational equivalence reflected in causal connections that remain undirected after the application of a causal search algorithm.

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Table 1. Classification of Approaches to Causality in Economics

	Structural	Process
<i>A Priori</i>	Cowles Commission: Koopmans (1953); Hood and Koopmans (1953)	Zellner (1979)
Inferential	Simon (1953) Hoover (1990, 2001) Favero and Hendry (1992) Natural Experiments: Angrist and Krueger (1999, 2001)	Granger (1969) Vector Autoregressions: (Sims 1980)