

**Graduate School Admissions (GSA).**<sup>1</sup> A graduate school became suspicious when it noticed a *negative correlation* between being female and being accepted (across *all* applicants in a given year). Further investigation revealed that — *within each department* — there was a *positive correlation* between being female and being accepted!

- Assume *two* departments:  $E$  and  $\bar{E}$  (think: *Easy & not-Easy*). Let  $M \stackrel{\text{def}}{=} \text{male}$ ,  $\bar{M} \stackrel{\text{def}}{=} \text{female}$  (gender binary),  $A \stackrel{\text{def}}{=} \text{accepted}$ , and  $\bar{A} \stackrel{\text{def}}{=} \text{rejected}$ . Finally, assume these *acceptance rates*.

	$M$	$\bar{M}$	Overall
$E$	60/80	40/50	100/130
$\bar{E}$	10/50	20/80	30/130
Overall	70/130	60/130	130/260

<sup>1</sup>This is a simplified version [10] of the example originally discussed in [2]. See [vudlab.com/simpsons/](http://vudlab.com/simpsons/) for some fun visualizations of this example.

- I'll offer a "rationalizing explanation" of *why* such examples may *seem* "paradoxical" shortly. First, I'll say some things about the existing literature on Simpson's Paradox (SP).
- The existing literature on SP tends to be concerned (almost exclusively) with doing the following two kinds of things.

1. Giving *mathematical explanations* (or *characterizations*) of the (algebraic) *structure* of SP cases. The  $2 \times 2$  case (as above), has a simple algebraic characterization [10].<sup>2</sup>
2. Giving *causal explanations* of the statistical distributions observed in *actual* SP cases [11]. In GSA, the causal story is simple (and benign). Females tend to apply to the "harder" department, *i.e.*, the department with lower acceptance rate.

- My aim is different — I want a "rationalizing explanation" of *why* SP may (reasonably) *seem paradoxical* in the first place.

<sup>2</sup>The probability calculus (a decidable algebraic theory [8]) can be used to provide a *general* characterization of the  $2 \times 2$  case. See Extras slides 11–12.

- There are various ways to try to explain (or *explain-away*) "paradoxicality." My approach fits the following mold [5].
  - **Step 1.** Identify the (or *an* explanatorily salient) argument form  $\mathcal{A}$  that is *invalidated* by the "paradoxical" cases.
  - **Step 2.** Identify a "similar" or "nearby" (more on this below) form of argument form  $\mathcal{A}^*$ , which is *universally valid*.
  - **Step 3.** Argue (or invite the listener to consider) that the (reasonable) *appearance* of paradoxicality stems (at least, in part) from *conflating*  $\mathcal{A}$  and  $\mathcal{A}^*$  — that is, from hearing examples of the "paradox" as invalidating argument form  $\mathcal{A}^*$  (which *would be* paradoxical, since  $\mathcal{A}^*$  is *valid*).
- Ideally, the argument forms  $\mathcal{A}$  and  $\mathcal{A}^*$  should:
  - (a) have sufficiently similar *logical forms*, and
  - (b) employ sufficiently similar (probabilistic) *concepts*.
- Moreover, ideally, the "explanation" should (c) be *fully general* (*i.e.*, be applicable to *all instances* of the "paradox").

- Carnap [1] distinguished two senses of "confirmation."
  - Confirmation as firmness.**  $P$  confirms <sub>$f$</sub>   $Q$ , on the (indicative) supposition that  $R$ , just in case  $Q$  is (sufficiently) *probable*, conditional upon the conjunction  $P \& R$ . Formally,

$$P \text{ confirms}_f Q, \text{ on the (indicative) supposition that } R \\ \text{iff} \\ \Pr(Q | P \& R) > t.^3$$

- Confirmation as increase in firmness.**  $P$  confirms <sub>$i$</sub>   $Q$ , on the (indicative) supposition that  $R$ , just in case  $P$  and  $Q$  are *positively correlated*, conditional upon  $R$ . Formally,

$$P \text{ confirms}_i Q, \text{ on the (indicative) supposition that } R \\ \text{iff} \\ \Pr(Q | P \& R) > \Pr(Q | \bar{P} \& R).$$

- Since our "explanation" of SP will be formal/universal, the *interpretation* of  $\Pr(\cdot | \cdot)$  can be allowed to vary, as needed.

<sup>3</sup>Here,  $t \geq 1/2$  is some (possibly contextually determined) *threshold*.

Example of SP ○	Confirmation-Theoretic "Explanation" of SP ○○●○○○○○	Extras ○○○○○	References
<ul style="list-style-type: none"> <li>● That brings us to <b>Step 1</b> of our "explanation." Here is the argument form <math>\mathcal{A}</math> that is invalidated by instances of SP.<sup>4</sup> <div style="margin-left: 20px;"> <p>(1) <math>P</math> confirms<sub><math>i</math></sub> <math>Q</math>, on the supposition that <math>R</math>.</p> <p>(<math>\mathcal{A}</math>) (2) <math>P</math> confirms<sub><math>i</math></sub> <math>Q</math>, on the supposition that <math>\bar{R}</math>.</p> <hr style="width: 80%; margin-left: 0;"/> <p>∴ (3) <math>P</math> confirms<sub><math>i</math></sub> <math>Q</math>, <i>unconditionally</i>.<sup>5</sup></p> </div> </li> <li>● In our GSA example, <math>\mathcal{A}</math> is instantiated as follows:           <div style="margin-left: 20px;"> <p>(1) <math>\bar{M}</math> confirms<sub><math>i</math></sub> <math>A</math>, on the supposition that <math>E</math>.</p> <p>(2) <math>\bar{M}</math> confirms<sub><math>i</math></sub> <math>A</math>, on the supposition that <math>\bar{E}</math>.</p> <hr style="width: 80%; margin-left: 0;"/> <p>∴ (3) <math>\bar{M}</math> confirms<sub><math>i</math></sub> <math>A</math>, <i>unconditionally</i>.</p> </div> </li> <li>● The Pr-distribution determined by our GSA <math>2 \times 2</math> table above constitutes a <u>counterexample</u> to the validity of <math>\mathcal{A}</math>.           <p style="margin-left: 20px;"><sup>4</sup>Strictly speaking, SP is more general than <math>\mathcal{A}</math>, since (i) it can also involve <i>disconfirmation<sub><math>i</math></sub></i> and/or <i>irrelevance</i>, and (ii) it can involve random variables with <i>more than two values</i>. My explanation(s) go through in full generality.</p> <p style="margin-left: 20px;"><sup>5</sup>Note: "unconditionally" just means "on a tautological supposition."</p> </li></ul>			
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Example of SP ○	Confirmation-Theoretic "Explanation" of SP ○○○○●○○○○	Extras ○○○○○	References																
<ul style="list-style-type: none"> <li>● To see this, we can add <i>probabilistic labels</i> to our GSA table.           <table border="1" style="margin: 10px auto; border-collapse: collapse; text-align: center;"> <thead> <tr style="border-top: 2px solid black; border-bottom: 2px solid black;"> <th style="border: none;"></th> <th style="border: none;"><math>M</math></th> <th style="border: none;"><math>\bar{M}</math></th> <th style="border: none;">Overall</th> </tr> </thead> <tbody> <tr> <td style="border: none;"><math>E</math></td> <td style="border: none;"><math>60/80 = \Pr(A   E \&amp; M)</math></td> <td style="border: none;"><math>40/50 = \Pr(A   E \&amp; \bar{M})</math></td> <td style="border: none;"><math>100/130 = \Pr(A   E)</math></td> </tr> <tr> <td style="border: none;"><math>\bar{E}</math></td> <td style="border: none;"><math>10/50 = \Pr(A   \bar{E} \&amp; M)</math></td> <td style="border: none;"><math>20/80 = \Pr(A   \bar{E} \&amp; \bar{M})</math></td> <td style="border: none;"><math>30/130 = \Pr(A   \bar{E})</math></td> </tr> <tr style="border-bottom: 2px solid black;"> <td style="border: none;">Overall</td> <td style="border: none;"><math>70/130 = \Pr(A   M)</math></td> <td style="border: none;"><math>60/130 = \Pr(A   \bar{M})</math></td> <td style="border: none;"><math>130/260 = \Pr(A)</math></td> </tr> </tbody> </table> </li> <li>● With these probabilistic labels in place, we can now see that:           <ol style="list-style-type: none"> <li>(1) <math>\Pr(A   E \&amp; M) &lt; \Pr(A   E \&amp; \bar{M})</math>. That is, <math>\bar{M}</math> confirms<sub><math>i</math></sub> <math>A</math>, on the supposition that <math>E</math>. In words: being female is <i>positively correlated</i> with acceptance, <i>in department E</i>.</li> <li>(2) <math>\Pr(A   \bar{E} \&amp; M) &lt; \Pr(A   \bar{E} \&amp; \bar{M})</math>. That is, <math>\bar{M}</math> confirms<sub><math>i</math></sub> <math>A</math>, on the supposition that <math>\bar{E}</math>. In words: being female is <i>positively correlated</i> with acceptance, <i>in department E</i>.</li> <li>(3) <math>\Pr(A   M) &gt; \Pr(A   \bar{M})</math>. That is, <math>\bar{M}</math> <i>disconfirms<sub><math>i</math></sub></i> <math>A</math>, <i>unconditionally</i>. In words: being female is <i>negatively correlated</i> with acceptance, <i>in the general population</i>.</li> </ol> </li> <li>● This explains, purely in confirmation<sub><math>i</math></sub> terms, what SP is.</li> </ul>					$M$	$\bar{M}$	Overall	$E$	$60/80 = \Pr(A   E \& M)$	$40/50 = \Pr(A   E \& \bar{M})$	$100/130 = \Pr(A   E)$	$\bar{E}$	$10/50 = \Pr(A   \bar{E} \& M)$	$20/80 = \Pr(A   \bar{E} \& \bar{M})$	$30/130 = \Pr(A   \bar{E})$	Overall	$70/130 = \Pr(A   M)$	$60/130 = \Pr(A   \bar{M})$	$130/260 = \Pr(A)$
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Example of SP ○	Confirmation-Theoretic "Explanation" of SP ○○○○○●○○○○	Extras ○○○○○	References
<ul style="list-style-type: none"> <li>● So much for <b>Step 1</b>. On to <b>Step 2</b>. I will examine <i>two</i> confirmation-theoretic (and 1 causal) "explanations" of SP.</li> <li>● <b>First Way</b>. This way involves a postulated simple conflation of Carnap's two senses of confirmation (note: this is a well-established human psychological conflation [3]).           <div style="margin-left: 20px;"> <p>(1) <math>P</math> confirms<sub><math>f</math></sub> <math>Q</math>, on the supposition that <math>R</math>.</p> <p>(<math>\mathcal{A}_1^*</math>) (2) <math>P</math> confirms<sub><math>f</math></sub> <math>Q</math>, on the supposition that <math>\bar{R}</math>.</p> <hr style="width: 80%; margin-left: 0;"/> <p>∴ (3) <math>P</math> confirms<sub><math>f</math></sub> <math>Q</math>, <i>unconditionally</i>.</p> </div> </li> <li>● <math>\mathcal{A}_1^*</math> is <i>universally valid</i>. This is easy to show, since it (essentially) boils down to the following "most" validity.<sup>6</sup> <div style="margin-left: 20px;"> <p>(1) Most <math>P</math> &amp; <math>R</math>-worlds are <math>Q</math>-worlds.</p> <p>(<math>\mathcal{A}_1^*</math>) (2) Most <math>P</math> &amp; <math>\bar{R}</math>-worlds are <math>Q</math>-worlds.</p> <hr style="width: 80%; margin-left: 0;"/> <p>∴ (3) Most <math>P</math>-worlds are <math>Q</math>-worlds.</p> </div> <p style="margin-left: 20px;"><sup>6</sup>See Extras slide 13 for a rigorous algebraic proof of the validity of <math>\mathcal{A}_1^*</math>.</p> </li> </ul>			
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Example of SP ○	Confirmation-Theoretic "Explanation" of SP ○○○○○●○○○○	Extras ○○○○○	References
<ul style="list-style-type: none"> <li>● <b>Second Way</b>. This way does not involve a simple conflation of Carnap's two senses of "confirms." It involves <i>only</i> confirmation as increase in firmness (confirms<sub><math>i</math></sub>).</li> <li>● This time, the conflation will involve what I will call <i>suppositional vs conjunctive</i> confirmation.</li> <li>● Here's an analogy to help get a grip on the distinction. Consider the following two indicative conditional forms:           <ol style="list-style-type: none"> <li>(I) If <math>R</math>, then if <math>P</math> then <math>Q</math>.</li> <li>(II) If <math>P</math> &amp; <math>R</math>, then <math>Q</math>.</li> </ol> </li> <li>● Many philosophers [9] have claimed that (I) and (II) are (in general) <i>equivalent</i>.<sup>7</sup> As such, many think conflating (I) and (II) is OK. Here's an analogous <i>confirmational</i> pair.           <ol style="list-style-type: none"> <li>(S) <math>P</math> confirms <math>Q</math>, on the supposition that <math>R</math>.</li> <li>(C) <math>P</math> &amp; <math>R</math> confirms <math>Q</math>, <i>unconditionally</i>.</li> </ol> <p style="margin-left: 20px;"><sup>7</sup>This equivalence is called <i>import-export</i>. See [7, 4, 6] for discussion.</p> </li> </ul>			
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- Interestingly,  $\mathcal{S}$  and  $\mathcal{C}$  are *equivalent* for  $\text{confirms}_f$ , but *not* for  $\text{confirms}_i$ . To see the former, simply apply the definition of  $\text{confirms}_f$  above (then the equivalence will be obvious).
- The fact that  $\mathcal{S}$  and  $\mathcal{C}$  are *not* equivalent for  $\text{confirms}_i$  is the key to our Second Way. To wit, here's my second  $\mathcal{A}^*$  form.
  - (1)  $P \ \& \ R$  confirms  $Q$ , *unconditionally*.
  - (2)  $P \ \& \ \bar{R}$  confirms  $Q$ , *unconditionally*. $\therefore$  (3)  $P$  confirms  $Q$ , *unconditionally*.

☞  $\mathcal{A}_2^*$  is *valid* for *both*  $\text{confirms}_f$  and  $\text{confirms}_i$ .<sup>8</sup>

- So, if (3) is false, then at least one of (1) and (2) must also be false. In our GSA example, we have the following contrast:
  - (S)  $\bar{M}$  confirms<sub>*i*</sub>  $A$ , *on the supposition that*  $\bar{E}$ .
  - (C)  $\bar{M} \ \& \ \bar{E}$  *does not* confirm<sub>*i*</sub>  $A$ , *unconditionally*.

<sup>8</sup>See Extras slides 13 and 14 for algebraic proofs of these claims.

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Example of SP ○ Confirmation-Theoretic "Explanation" of SP ○○○○○○● Extras ○○○○ References

- How do our Two Ways fare wrt our three *desiderata* (a)–(c)?
- $\mathcal{A}_1^*$  (a) has *the same* logical form as  $\mathcal{A}$ , (b) involves *two* confirmational concepts (but those concepts are conflated in other contexts [3, 4]), and (c) covers *all* SP cases.
- $\mathcal{A}_2^*$  (a) has a *different* logical form than  $\mathcal{A}$  (but the two forms are conflated in other contexts [9, 4]), (b) involves *only one* confirmational concept, and (c) covers *all* SP cases.
- Finally, let's consider Pearl's *causal* approach to SP [11], which can be fit into our mold (see Extras slide 15 for details).
- Pearl's  $\mathcal{A}^*$  (a) has *almost* the same logical form as  $\mathcal{A}$  (if you think of Pearl's  $\mathcal{A}^*$  as an *enthymeme*), but (b) it involves *causal* and not merely probabilistic/confirmational concepts, and (c) because it (*sensu strictu*) requires an extra premise (*viz.*,  $P$  and  $R$  are "causally independent," in Pearl's sense), it does *not* apply to *all* cases of SP. [Note: I do not mean to deny that Pearl's story has explanatory value.]

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Example of SP ○ Confirmation-Theoretic "Explanation" of SP ○○○○○○○○ Extras ●○○○○ References

- The following *stochastic truth table* [8] represents all possible probability distributions over the  $\{P, Q, R\}$  language, *via* the 7 real variables  $a, b, c, d, e, f, g \in [0, 1]$ .

$P$	$Q$	$R$	$\Pr(\cdot)$
T	T	T	$a$
T	T	⊥	$b$
T	⊥	T	$c$
T	⊥	⊥	$d$
⊥	T	T	$e$
⊥	T	⊥	$f$
⊥	⊥	T	$g$
⊥	⊥	⊥	$1 - (a + b + c + d + e + f + g)$

- *In general*, an SP reversal (like our GSA reversal) occurs when the following three inequalities are satisfied.
 
$$\Pr(Q \mid P \ \& \ R) < \Pr(Q \mid \bar{P} \ \& \ R)$$

$$\Pr(Q \mid P \ \& \ \bar{R}) < \Pr(Q \mid \bar{P} \ \& \ \bar{R})$$

$$\Pr(Q \mid P) > \Pr(Q \mid \bar{P})$$

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Example of SP ○ Confirmation-Theoretic "Explanation" of SP ○○○○○○○○ Extras ○●○○○ References

- Algebraically [8], these three SP inequalities become:
 
$$\frac{a}{a+c} < \frac{e}{e+g}$$

$$\frac{b}{b+d} < \frac{f}{1 - (a + b + c + d + e + g)}$$

$$\frac{a+b}{a+b+c+d} > \frac{e+f}{1 - (a + b + c + d)}$$
- It is easy to use PrSAT [8] to find *instances* of this pattern (or *any* SP pattern). But, giving a general characterization is quite complex (although, in principle, it is decidable).
- In any case, this does constitute a *general*, algebraic characterization of (dichotomous) SP reversals (which subsumes the case involving statistical frequencies, expressible in terms of  $2 \times 2$  contingency tables).
- The next two slides contain (algebraic) proofs of the validity of  $\mathcal{A}_1^*$  and  $\mathcal{A}_2^*$  (using this same algebraic setup).

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Example of SP ○	Confirmation-Theoretic "Explanation" of SP ○○○○○○○○○	Extras ○○●○○	References
<ul style="list-style-type: none"> <li>● <i>Probabilistically</i>, <math>\mathcal{A}_1^*</math> is (by definition) as follows.               <div style="margin-left: 20px;"> <math display="block">(1) \Pr(Q   P \ \&amp; \ R) &gt; t.</math> </div> <math display="block">(\mathcal{A}_1^*) \frac{(2) \Pr(Q   P \ \&amp; \ \bar{R}) &gt; t.}{\therefore (3) \Pr(Q   P) &gt; t.}</math> </li> <li>● <i>Algebraically</i> (using the above setup [8]), <math>\mathcal{A}_1^*</math> becomes:               <div style="margin-left: 20px;"> <math display="block">(1) \frac{a}{a+c} &gt; t.</math> </div> <math display="block">(\mathcal{A}_1^*) \frac{(2) \frac{b}{b+d} &gt; t.}{\therefore (3) \frac{a+b}{a+b+c+d} &gt; t.}</math> </li> <li>● Cross-multiplying (1) &amp; (2) yields:               <div style="margin-left: 20px;"> <math display="block">(1) \quad \quad \quad a &gt; (a + c) \cdot t</math> <math display="block">(2) \quad \quad \quad b &gt; (b + d) \cdot t</math> </div> </li> <li>● Adding the lhs &amp; rhs of these and collecting <math>t</math> yields (3). <math>\square</math> <math display="block">(3) \quad \quad \quad a + b &gt; (a + b + c + d) \cdot t</math> </li> </ul>			13

Example of SP ○	Confirmation-Theoretic "Explanation" of SP ○○○○○○○○○	Extras ○○○●	References
<ul style="list-style-type: none"> <li>● Here is Pearl's argument form: <math>\mathcal{A}_{\mathcal{P}}^*</math>.               <div style="margin-left: 20px;"> <math display="block">(0) \Pr(R   do(P)) = \Pr(R   do(\bar{P})) = \Pr(R).</math> </div> <math display="block">(\mathcal{A}_{\mathcal{P}}^*) \frac{(1) do(P) \text{ confirms}_i Q, \text{ on the supposition that } R.}{(2) do(P) \text{ confirms}_i Q, \text{ on the supposition that } \bar{R}.}</math> <math display="block">\therefore (3) do(P) \text{ confirms}_i Q, \text{ unconditionally.}</math> </li> <li>● If we think of it as an <i>enthymeme</i> — with premise (0) left <i>unstated</i> — then its form is <i>almost</i><sup>10</sup> the same as <math>\mathcal{A}</math>.</li> <li>● Premise (0) asserts that <math>P</math> is <i>casually independent</i> of <math>R</math>.</li> <li>● In GSA, premise (0) says that <i>intervening on an applicant's gender would not affect the probability that she applies to department E, as opposed to department <math>\bar{E}</math>.</i></li> <li>● That seems right. But, there are cases in which (0) <i>fails</i>, but SP occurs (and can still seem, to some extent, "paradoxical").</li> </ul> <p><sup>10</sup>In (1)-(3), <math>do(P)</math> needs to be contrasted with <math>do(\bar{P})</math>, not <math>\bar{do}(P)</math>, and so the actual form of Pearl's <math>\mathcal{A}_{\mathcal{P}}^*</math> is slightly different than what I've written here.</p>			15

Example of SP ○	Confirmation-Theoretic "Explanation" of SP ○○○○○○○○○	Extras ○○●○○	References
<ul style="list-style-type: none"> <li>● <i>Probabilistically</i>, <math>\mathcal{A}_2^*</math> is <i>equivalent to</i><sup>9</sup> the following.               <div style="margin-left: 20px;"> <math display="block">(1) \Pr(Q   P \ \&amp; \ R) &gt; \Pr(Q).</math> </div> <math display="block">(\mathcal{A}_2^*) \frac{(2) \Pr(Q   P \ \&amp; \ \bar{R}) &gt; \Pr(Q).}{\therefore (3) \Pr(Q   P) &gt; \Pr(Q).}</math> </li> <li>● <i>Algebraically</i> (using the above setup [8]), <math>\mathcal{A}_1^*</math> becomes:               <div style="margin-left: 20px;"> <math display="block">(1) \frac{a}{a+c} &gt; a + b + e + f.</math> </div> <math display="block">(\mathcal{A}_2^*) \frac{(2) \frac{b}{b+d} &gt; a + b + e + f.}{\therefore (3) \frac{a+b}{a+b+c+d} &gt; a + b + e + f.}</math> </li> <li>● Cross-multiplying (1) &amp; (2) yields:               <div style="margin-left: 20px;"> <math display="block">(1) \quad \quad \quad a &gt; (a + c) \cdot (a + b + e + f)</math> <math display="block">(2) \quad \quad \quad b &gt; (b + d) \cdot (a + b + e + f)</math> </div> </li> <li>● Adding the lhs &amp; rhs of these and collecting <math>t</math> yields (3). <math>\square</math> <math display="block">(3) \quad \quad \quad a + b &gt; (a + b + c + d) \cdot (a + b + e + f)</math> </li> </ul> <p><sup>9</sup>This formulation allows us to prove <math>\mathcal{A}_2^*</math> in <i>the same way</i> we proved <math>\mathcal{A}_1^*</math>.</p>			14

Example of SP ○	Confirmation-Theoretic "Explanation" of SP ○○○○○○○○○	Extras ○○○○	References
<ul style="list-style-type: none"> <li>[1] R. Carnap, <i>Logical Foundations of Probability</i>, 1962. (<a href="http://fitelson.org/carnap/logical_foundations_of_probability.pdf">http://fitelson.org/carnap/logical_foundations_of_probability.pdf</a>)</li> <li>[2] N. Cartwright, "Causal laws and effective strategies," 1979. (<a href="http://fitelson.org/Cartwright_CLAES.pdf">http://fitelson.org/Cartwright_CLAES.pdf</a>)</li> <li>[3] V. Crupi, B. Fitelson and K. Tentori, "Probability, confirmation, and the conjunction fallacy," 2008. (<a href="http://fitelson.org/pccf.pdf">http://fitelson.org/pccf.pdf</a>)</li> <li>[4] I. Douven, <i>The Epistemology of Indicative Conditionals</i>, 2016. (<a href="http://tiny.cc/mir8cy">http://tiny.cc/mir8cy</a>)</li> <li>[5] B. Fitelson and J. Hawthorne, "The Wason Task(s) and the Paradox of Confirmation," 2010. (<a href="http://fitelson.org/wason.pdf">http://fitelson.org/wason.pdf</a>)</li> <li>[6] B. Fitelson, "Comments on Khoo &amp; Mandelkern," 2017. (<a href="http://fitelson.org/kmc.pdf">http://fitelson.org/kmc.pdf</a>)</li> <li>[7] _____, "Two New(ish) Triviality Results for the Indicative Conditional," 2016. (<a href="http://fitelson.org/triviality_handout.pdf">http://fitelson.org/triviality_handout.pdf</a>)</li> <li>[8] _____, "A decision procedure for probability calculus with applications," 2008. (<a href="http://fitelson.org/pm.pdf">http://fitelson.org/pm.pdf</a>)</li> <li>[9] A. Gillies, "Indicative Conditionals," 2014. (<a href="http://fitelson.org/gillies_ic.pdf">http://fitelson.org/gillies_ic.pdf</a>)</li> <li>[10] G. Malinas and J. Bigelow, "Simpson's Paradox," 2016. (<a href="http://plato.stanford.edu/archives/sum2016/entries/paradox-simpson/">http://plato.stanford.edu/archives/sum2016/entries/paradox-simpson/</a>)</li> <li>[11] J. Pearl, "Simpson's Paradox: An Anatomy," 2011. (<a href="http://fitelson.org/pearl_sp.pdf">http://fitelson.org/pearl_sp.pdf</a>)</li> </ul>			16