

LOGICAL FOUNDATIONS OF EVIDENTIAL SUPPORT

Branden Fitelson^{*†}

Abstract

Carnap's inductive logic (or confirmation) project is revisited from an "increase in firmness" (or probabilistic relevance) point of view. It is argued that Carnap's main desiderata can be satisfied in this setting, without the need for a theory of "logical probability". The emphasis here will be on explaining how Carnap's epistemological desiderata for inductive logic will need to be modified in this new setting. The key move is to abandon Carnap's goal of bridging confirmation and *credence*, in favor of bridging confirmation and *evidential support*.

^{*}Department of Philosophy, University of California-Berkeley, 314 Moses Hall #2390, Berkeley, CA 94720-2390

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1 Setting the Stage: Three Carnapian Desiderata

In the second edition of *Logical Foundations of Probability* (LFP), Carnap (1962, xvi) distinguished two kinds of inductive-logical confirmation relations: *confirmation as firmness*, which he informally characterized as “How probable the hypothesis H is on the basis of the evidence E ”, and *confirmation as increase in firmness*, which he informally characterized as “How much the probability of H is increased when new evidence E is acquired (in addition to the prior evidence which, for simplicity, we shall take here as tautological).” Carnap devotes almost all of LFP to the task of explicating the former. Presently, I will discuss Carnap’s approach to the former, and sketch my own approach to the latter. My discussion will focus, ultimately, on the relation between inductive logic (the confirmation as increase in firmness relation), and epistemology (the relation of incremental evidential support).

I begin with some quotes from LFP to set the stage. The first gives a general sense of the very idea of inductive logic, as a quantitative analogue (or generalization) of deductive logic:

Deductive logic may be regarded as the theory of the relation of logical consequence \vdash , and inductive logic as the theory of another concept ϵ which is likewise objective and logical ... degree of confirmation.

The next two quotes give Carnap’s (1962, 200) informal characterizations of the terms “logical” and “objective” as they apply to the relations \vdash and ϵ :

The principal common characteristic of the statements in both fields is their independence of the contingency of facts. This characteristic justifies the application of the common term ‘logic’ to both fields.

That ϵ is an objective concept means this: if a certain ϵ value holds for a certain hypothesis with respect to a certain evidence, then this value is entirely independent of what any person may happen to think about these sentences.

It is clear that Carnap, at least, intends here to be saying that statements of confirmation theory should be *analytic*. But, *mere analyticity* is not all that is required of confirmation theory. Confirmation (ϵ) must be analogous to entailment (\vdash) in certain *other* ways as well. Specifically, Carnap (1962, 202) adds:

They both involve the concept of range. ‘ E L-implies H ’ [$E \vdash H$] means that the entire range of E is included in that of H , while ... ‘ $\epsilon(H, E) = 3/4$ ’ means three-fourths of the range of E is included in that of H .¹

Moreover, Carnap emphasizes that both relations (\vdash and ϵ) should be applicable to *epistemology* in analogous ways. He endorses analogous *epistemic bridge principles* for both relations. For the \vdash relation, Carnap (1962, 201) endorses the following closure principle:

¹Here, Carnap has in mind confirmation as *firmness*. We’ll have to generalize this ‘range’ analogy with entailment when we discuss confirmation as *increase in firmness*, below.

If E is known by the person X at the time t , then H is likewise known by X at t [provided that $E \vdash H$ is also known by X at t].

For c , Carnap (1962, 201) endorses the following principle, which he takes to be *analogous* to closure:

If E and *nothing else* is known by X at t , then the degree of belief justified by the knowledge of X at t is $3/4$ [provided that $c(H, E) = 3/4$ is also known by X at t].

For Carnap, then, inductive logic involves a confirmation relation c which has (at least) the following three characteristics (I take these to be neutral between the firmness and increase in firmness conceptions of confirmation):

- *Analyticity*: Statements involving c should be *analytic*, like statements involving \vdash are.
 - Carnap had a philosophical theory of analyticity. We won't worry too much here about the details of his theory of analyticity (since that is not our emphasis). Roughly, here we will (following the spirit of Carnap's informal characterizations of analyticity rather than the letter of his technical theory thereof) take 'analytically true' to mean 'true in the way that (true) mathematical statements are true'.
- *Logicity*: c should be a *quantitative generalization* of \vdash .
 - $c(H, E)$ should be maximal (minimal) when $E \vdash H$ ($E \vdash \sim H$).²
- *Applicability*: c should be *applicable to epistemology* in ways analogous to the ways in which \vdash is applicable to epistemology.
 - Some kind of *epistemic bridge principle(s)* should hold, which connects c with some epistemic concept (much more on this below).³

2 Carnap's Approach to Confirmation as Firmness

Carnap's $c(\cdot, \cdot)$ s are, basically, measures of the relative frequencies with which certain syntactical particles occur in the sentences of certain simple formal languages.⁴ The building blocks of early Carnapian c s are "regular logical measure

²That is, so long as the function $c(H, E)$ is *defined*. I am ignoring the paradoxes of entailment (see below). I have generalized Carnap's "logical range" analogy, since that analogy breaks down when we are talking about *increase in firmness*. I have settled on this desideratum, since it is the strongest one I can think of that is capable of meaningfully applying to both the firmness and the increase in firmness conceptions of confirmation.

³As we will see below, Carnap has other epistemic applicability requirements in mind, which go beyond mere "epistemic bridge principles". I won't comment too much on these additional desiderata here, as this would require a much longer and involved treatment.

⁴Here, I have in mind Carnap's early writings on confirmation and inductive logic. Later on, he moved toward a more semantical approach and away from the early syntactical approaches to confirmation. This distinction is not terribly important for present purposes. So, because it is simpler to talk about Carnap's early approaches, that's what I will do. For a more in-depth discussion of Carnap's programme along present lines, see (Fitelson 2005).

functions” $m(\cdot)$. Such m s assign numbers on $(0, 1)$ (which sum to 1) to each of the *state descriptions* (\mathfrak{S}) of some (monadic) first-order language \mathcal{L} . In his earliest system, Carnap uses $m^\dagger(\cdot)$, which assigns *equal measure* to each *state description* in \mathcal{L} . Conditional “logical” probability (c^\dagger) is then given by a *ratio* of these unconditional “logical” probabilities (in the usual way): $c^\dagger(H, E) = \frac{m^\dagger(H \& E)}{m^\dagger(E)}$. This function c^\dagger satisfies the first two desiderata, above, because: (i) c^\dagger statements are *analytic*, since, *given* m^\dagger , they are determined by the structure of \mathcal{L} , and (ii) c^\dagger *generalizes entailment*, since c^\dagger is maximal (minimal) when $E \vdash H$ ($E \vdash \sim H$).⁵ Nonetheless, Carnap eventually *rejects* c^\dagger , because he thinks its *applicability to epistemology* is unsatisfactory. Interestingly, this is *not* because c^\dagger fails to undergird his desired epistemic bridge principle. Carnap (1962, 565) explains:

The choice of c^\dagger as the degree of confirmation would be tantamount to the principle never to let our past experiences influence our expectations for the future.

What Carnap *means* here is that, according to $c^\dagger(H, E)$, no E can ever *increase the firmness* of any H (unless $E \vdash H$). That is, we can never have $c^\dagger(H, E) > c^\dagger(H, \top)$, unless $E \vdash H$.⁶

Because of this “no learning from experience problem”, Carnap abandons c^\dagger in favor c^* : a function constructed using a *different* measure function m^* , which assigns equal measure to the *structure descriptions* (\mathfrak{Str}) of \mathcal{L} . The structure descriptions of \mathcal{L} are just collections of state descriptions of \mathcal{L} that are invariant under permutations of individual constants. This “clumping” of state descriptions avoids the “no learning from experience” problem. But, Carnap thinks c^* has other shortcomings concerning its epistemic applicability. This causes Carnap to add an *adjustable parameter* λ to his c -constructions, which yields a λ -continuum of c -functions.⁷ Later, Carnap puzzled over still other epistemic application requirements that he thought no c_λ -function could adequately meet. This led to the addition of further adjustable parameters to his systems, which allowed Carnap more flexibility in the ways he could carve up his languages \mathcal{L} . But, even this broader class of c s never seemed fully satisfactory to Carnap from the point of view of its epistemic applicability. In the end, the classes of probability functions that one can construct Carnap-style from such \mathcal{L} s don’t seem rich enough to meet all the demands of general epistemic application (Maher 2001).

⁵Carnap’s c s get more than just the “endpoints” right, they give a tighter quantitative generalization in terms of “logical range”. This cannot be achieved by measures of confirmation as increase in firmness. See (Kemeny & Oppenheim 1952) for similar remarks.

⁶It is somewhat strange that Carnap should see *this* as a problem for a measure of confirmation as *firmness*. But, I’ll let that pass. Carnap (in the early days) had a tendency to slide back and forth between considerations of firmness confirmation and considerations of increase in firmness confirmation. See (Michalos 1971) for an extended discussion of this aspect of Carnap’s thought, and Popper’s criticisms of it.

⁷Basically, λ is an *index of caution*. If λ is infinite, then no learning from experience is possible: c^\dagger , and if λ is set to a certain finite value, then it yields c^* , etc.

At this point, the following two key questions come to mind:

- Why bother with such syntactical constructions in the first place?
- *Can we have analyticity, logicity, and epistemic applicability?*

In the next two sections, I will explain how we can avoid bothering with Carnap-style logical constructions while preserving all three Carnapian desiderata.

3 Analyticity and Logicity on the Cheap

Carnap acts as if the *analyticity* of ϵ *requires* its syntactical construction (within \mathcal{L}) out of “logical measure functions”. It’s unclear why this should be true (*even if* you accept Carnap’s formalistic understanding of analyticity). There seems to be an additional presupposition at work here: that the function ϵ should be *two-place* in the same way that \vdash is two-place. But, the attempt to construct a two-place ϵ seems to have failed. Even Carnap found the need to add *adjustable* parameters to his recipes for constructing ϵ s. And, the resulting ϵ statements will not even be *determinate* (much less analytic) until all of these parameters are *adjusted* (and even Carnap concedes that – in general – they cannot be adjusted *a priori*). So, in the end, ϵ isn’t *really* two-place, even for Carnap. I suggest another (more direct and general) way to ensure analyticity:

- ϵ is a *three-place* relation between E , H , and *a probability model* (or a family thereof) \mathcal{M} .⁸

By making ϵ explicitly a three-place relation in this way, we don’t restrict ourselves to a *limited class* of probability models that can be cooked-up using simple first-order languages \mathcal{L} according to some Carnapian recipe. This is advantageous, because there are many probability models which seem salient to statistical and inductive inference that cannot be simulated by even the most sophisticated of Carnapian constructions (Maher 2001). Moreover, this (obviously) yields *analyticity* (even in Carnap’s technical sense), since *given* \mathcal{M} , all probability statements — *relative to* \mathcal{M} — are *mathematically true*.⁹ So, we

⁸By a *probability model*, I mean a boolean algebra of propositions, together with a function satisfying whichever axioms for probability you prefer. I prefer Kolmogorov’s (1933) axioms for probability, but others prefer to take conditional probability as primitive. See (Hájek 2003). This issue is not crucial for my present purposes (especially in light of the fact that I am ignoring cases in which E and/or H are non-contingent), and so I will remain neutral on it here.

⁹One might object that this gets us analyticity *too* cheaply. After all, in this sense the mathematical statements of mathematical physics can also be considered analytic (once we relativize them to concrete mathematical structures). This may be true, but a mathematical theory of physics needs to be more than just analytic in this sense (*i.e.*, in the sense that its mathematical claims are analytic *qua* mathematical claims) — it also needs to be *empirically adequate*, *etc.* Likewise, theories of confirmation also need to satisfy *logicity* and *applicability*. So, the fact that analyticity is “cheap” in this way does not, to my mind, undermine the philosophical significance of inductive logic so understood. One of the reasons Carnap wanted the statements in his theory of confirmation to be analytic is that he wanted them (if true) to be knowable *a priori*. I don’t see how this is possible if the statements aren’t even *determinate* until certain adjustable parameters are fixed *empirically* (as in Carnap’s systems). By getting analyticity “on the cheap”, we avoid this problem. A complete response to this objection is beyond the scope of the present discussion.

can easily obtain *analyticity* (and increased generality) by making \mathfrak{c} three-place rather than two-place. How about *logicality*? Yep. That’s not a problem either, since, in *all* probability models \mathcal{M} (Carnapian or otherwise), $\text{Pr}_{\mathcal{M}}(H | E)$ will be maximal (minimal) when $E \vdash H$ ($E \vdash \sim H$).

However, when we make the three-place nature of \mathfrak{c} explicit, the *epistemic applicability* problem becomes prominent. To see this, consider the following naïve, \mathcal{M} -relativized Carnap-style bridge principle for *firmness* and *credence*:

If X knows E and nothing else (*a posteriori*), and X knows (*a priori*) that $\text{Pr}_{\mathcal{M}}(H | E) = r$, then X ’s *credence* in H , given E , should be r .

This just *can’t* be true, since if it were true, then nothing about the *relationship between* the model \mathcal{M} , the agent X , and/or the world would be required to constrain X ’s credences.¹⁰ Hence, this principle would be implausible *even if* we had an understanding of what it means (in general) to “know E and nothing else.” What made Carnap’s bridge principle *at all* plausible (perhaps *modulo* the “and nothing else” clause) was that *his* models were supposed to *be models of* “*a priori* probability”. As such, they had their epistemic credentials *built-in* to them from the start. But, what if *there is no such thing* as “logical” or “*a priori*” probability (as many of us now suspect)? Does this mean that inductive logic is impossible? Not necessarily. At least, that’s what I will try to argue.

4 Confirmation as Increase in Firmness Revisited

Let’s return to confirmation as *increase in firmness* now. It is well-known (Fitzelson 2001) that there are *many* measures of “the degree to which E increases the firmness of H .” Interestingly, very few of these satisfy *logicality*. We can sum-up the desiderata of logicality and “sensitivity to increase in firmness (or relevance),” as follows. For all *contingent*¹¹ E and H :

$$\mathfrak{c}(H, E, \mathcal{M}) \text{ should be } \left\{ \begin{array}{ll} \text{Maximal} & \text{if } E \text{ entails } H. \\ > 0 & \text{if } E \text{ and } H \text{ are } \textit{correlated} \text{ in } \mathcal{M}. \\ = 0 & \text{if } E \text{ and } H \text{ are } \textit{independent} \text{ in } \mathcal{M}. \\ < 0 & \text{if } E \text{ and } H \text{ are } \textit{anti-correlated} \text{ in } \mathcal{M}. \\ \text{Minimal} & \text{if } E \text{ entails } \sim H. \end{array} \right.$$

As it turns out, of all the *relevance measures* used or defended in the historical literature on confirmation (up to ordinal equivalence), only $l(H, E, \mathcal{M}) = \log \left[\frac{\text{Pr}_{\mathcal{M}}(E | H)}{\text{Pr}_{\mathcal{M}}(E | \sim H)} \right]$ and $l'(H, E, \mathcal{M}) = \log \left[\frac{\text{Pr}_{\mathcal{M}}(H | E)}{\text{Pr}_{\mathcal{M}}(H | \sim E)} \right]$ satisfy logicality.¹² And, if

¹⁰This is tantamount to treating *arbitrary* Pr-functions as “expert probabilities” (Gaifman 1988).

¹¹Cases in which E and/or H are not contingent are very tricky — even in *deductive* logic (*e.g.*, the paradoxes of entailment). So, for simplicity, I will bracket those cases here.

¹²This fact about l was known to Kemeny & Oppenheim (1952), who are (strangely) not cited by Carnap (1962) in his discussion of confirmation as increase in firmness. What I am doing here differs from what Kemeny & Oppenheim were doing in at least two respects. First, they were still working with Carnap-style theories of “logical probability”, which I have abandoned. And, second, they do not discuss the problem of epistemic applicability, which is a crucial problem that any adequate account of inductive logic must address.

we impose the following additional constraint (which seems to be accepted by all historical practitioners of probabilistic confirmation theory):

$$\text{If } \Pr_{\mathcal{M}}(H | E_1) \geq \Pr_{\mathcal{M}}(H | E_2), \text{ then } c(H, E_1, \mathcal{M}) \geq c(H, E_2, \mathcal{M}).$$

then, we get *historical uniqueness* of l .¹³ That's neat. But, I don't want make too much of fuss here about *quantitative* relevance confirmation claims of the form ' $c(H, E, \mathcal{M}) = r$ ', since I think the most objective claims (and the claims most analogous to entailment claims) are *qualitative* claims of the form ' $c(H, E, \mathcal{M}) \geq 0$ '. Are there bridge principles relating the qualitative *increase in firmness* confirmation relation an some epistemically important relation? I think so. But, these principles will *not* bridge confirmation as increase in firmness and *credence* (since confirmation as increase in firmness measures are not *probability* functions). Rather, they will bridge confirmation and (incremental) *evidential support*. Moreover, I suspect that there are also *comparative* bridge principles, which bridge comparative confirmation claims and comparative claims about evidential support (but these will be more controversial). Let's look at the qualitative case first.

It's useful here to compare the deductive and inductive cases. In the deductive case, the bridge-principle is rather simple. If a rational agent knows $E \vdash H$ and E , then (*ceteris paribus*)¹⁴ they may be said to know H on the basis of E . Figure 1 allows us to picture a concrete example. In Figure 1, our agent learns *a posteriori* that (E) a card drawn at random from a standard deck is the ace of spades, and they know *a priori* that E entails (H) the card is a spade. So, the agent may (*ceteris paribus*) be said to know that H on the basis of E . The important thing to note here is that *we may ignore the stochastic properties of the process which generated E* . It doesn't matter whether our typical model of random card draws is a correct model of the process which generated E . Because the agent knows that E entails H in this case, the agent will know H on the basis of E here *independently* of such considerations. Carnap wanted the same kind of independence to obtain when it comes to inductive-logical bridge principles. In other words, he wanted the inductive-logical picture to look as

¹³By "historical uniqueness", I mean only that l (or its ordinal equivalents) are the only *historically proposed and/or defended* measures (up to ordinal equivalence) which satisfy all of our present desiderata. To get *mathematical* uniqueness, one would need to make some rather strong continuity assumptions, which have no intuitive connection to material desiderata for inductive logic. Such dubious mathematical assumptions are used by Good (1960) and Milne (1996) for precisely this purpose. See (Halpern 1999) for a nice critical discussion of these sorts of arguments and the implausibility of the continuity assumptions they require. I prefer not to appeal to any such purely mathematical conditions, which cannot be seen as material desiderata for inductive logic. This is why I talk in terms of historical uniqueness rather than mathematical uniqueness. I am open to the possibility that additional material desiderata will be discovered which will narrow the field even further. That, it seems to me, is how scientific investigation should work.

¹⁴I don't mean to endorse a totally naïve closure principle for knowledge. This is a principle Carnap endorsed, and I am merely trying to tell a "Carnap-style" story here about firmness vs increase in firmness confirmation. To make this bridge principle more plausible, we would need to add various caveats, of course. I won't worry too much about such caveats here. All I need to assume is that there is *some* plausible bridge principle *in the vicinity* of this naïve one, and I think this is not such an implausible assumption. See (Hawthorne 2004) for a nice contemporary discussion (and defense) of deductive closure principles in epistemology.

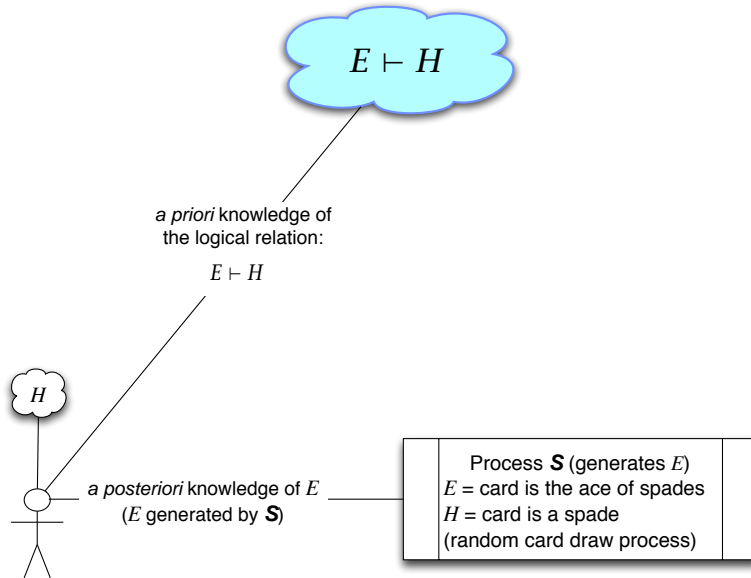


Figure 1: Entailment and knowledge

simple as our Figure 1. As I have implied above, I think *that* dream of Carnap's cannot be achieved. I think things just aren't so tidy in the case of inductive-logical bridge principles. That is, I think it is all but hopeless to have anything like the sort of bridge principle Carnap wanted (as stated above) for for confirmation *as firmness and credence*. I am skeptical here (mainly) for two reasons. First, I don't know what it *means* for an agent to "know E and nothing else (*a posteriori*)".¹⁵ Second, such a principle would seem to require the existence of objective, "*a priori* probabilities", and I don't think there are such things. That's the bad news. The good news is that I think we can avoid these problems when it comes to bridging confirmation as *increase in firmness* and *evidential support*. I will argue that bridging *these* concepts does *not* require *either* a "and the agent knows nothing else *a posteriori*" clause *or* the existence of objective "*a priori* probabilities". But, some additional complexity will be required in the inductive case, because in the inductive case *the nature of the stochastic process that generates E cannot be ignored*. Again, it helps to picture the sort of case I have in mind. Figure 2 depicts an agent who learns *a posteriori* that (E) a card drawn at random from a standard deck is either a 10 or a Jack, and they know *a priori* that — *in the standard probability model \mathcal{M} used to model random card draws* — E is *positively correlated* with (H) the card is a face card.

¹⁵Indeed, one might reasonably wonder how it is even *possible* for E to be the agent's *only a posteriori* knowledge, when their knowledge is supposed to be closed under logical consequence in accordance with the deductive bridge principle that Carnap himself endorsed.

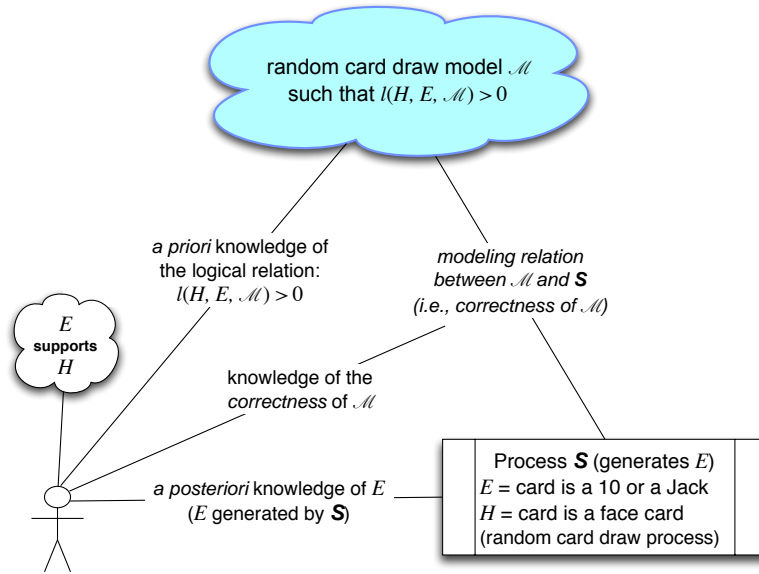


Figure 2: Qualitative confirmation and evidential support

I submit that in such cases the agent knows (*ceteris paribus*¹⁶) that E evidentially supports H — provided that the agent also knows that the model \mathcal{M} is a correct model of the stochastic process S that generated the event E . That is, I am suggesting the following bridge principle (or inference rule) relating *confirmation as increase in firmness* and *evidential support*:

a knows (*a posteriori*) that E by observing the outcome of a stochastic process S .
 a knows (*a priori*) that E confirms (increase in firmness sense) H in the model \mathcal{M} .
 a knows (*a posteriori*) that \mathcal{M} is a *correct*¹⁷ model of the stochastic process S .

 $\therefore a$ knows that E evidentially supports H .

¹⁶As in the deductive case, there are bound to be caveats required to make this bridge principle plausible. I won't try to articulate any of these here. This is a task for a longer treatise on inductive logic (I hope to articulate some of these in my book on inductive logic).

¹⁷A fair amount of metaphysical and epistemological work needs to go into this step. First, we need to say what it *means* for a probability model to be *correct* concerning a stochastic process, and second we need to say how we could come to *know* this. Presumably, the former would involve a story about the metaphysics of stochastic processes, and the latter would involve a delicate story about the epistemology of probability (delicate because there is the threat of a regress here, if we are inclined to be *evidentialists* about the knowledge of model-correctness itself). I will bracket these issues here, since this paper is mainly concerned with formulating *prima facie* plausible inductive-logical/epistemic bridge principles, not providing a complete story about probabilistic metaphysics and epistemology.

I think there are lots of examples illustrating the plausibility of the bridge principle stated above (and implicitly pictured in Figure 2).¹⁸ For instance, when a pregnancy test (S) which is known to be reliable is administered (properly, and on an appropriate individual, *etc.*), the observation of a positive test result (E) constitutes evidence in favor of pregnancy (H). This sort of example fits the mold of our bridge principle perfectly. In such cases, the observation is of (E) an event generated by a stochastic process S , and in the probability model \mathcal{M} of S which we know (let us assume) to be correct, there is a large positive likelihood-ratio $l(H, E, \mathcal{M})$. Such cases are canonical ones in which we are inclined to infer that E constitutes strong evidence in favor of H . Indeed, these are precisely the kinds of cases that statisticians use to illustrate how we should interpret the evidential import of the outcomes of stochastic processes (Royall 1997). As such, whereas Carnap was trying to provide a logical foundation for *credence* (or epistemic *probability*), we can now be seen to be aiming for a logical foundation for *evidential support*. I suspect that one of the reasons our increase in firmness/evidential support bridge principles are more plausible than their firmness/credence counterparts is that evidential relations are less sensitive to prior probabilities or background knowledge than credences are. See *fn.* 18 below and (Fitelson 2006) for further discussion of this issue.

Finally, I would like to say something about the prospects of formulating bridge principles relating *comparative confirmation* (as increase in firmness) and *comparative evidential support*. This case is more controversial, because the content of any such principle will depend sensitively the *ordinal structure* of one's particular measure of confirmation (as increase in firmness). And, there is widespread ordinal (or comparative) disagreement between such measures (Fitelson 2001). Nonetheless, I think such principles can be formulated. Figure 3 illustrates how I think such principles would work. In this example, our agent learns *a posteriori* that (E) a card drawn at random from a standard deck is an ace, and they know *a priori* that — *in the standard probability model* \mathcal{M} used to model random card draws — $l(H_1, E, \mathcal{M}) > l(H_2, E, \mathcal{M})$, where H_1 is the hypothesis that the card is either the ace of spades or the ace of diamonds, and H_2 is the hypothesis that the card is the ace of clubs. I submit

¹⁸It seems to me that the most compelling of these involve cases where the notion of “evidential support” is of an *objective/externalist* nature. I think this bridge principle is harder to defend from a purely *subjective/internalist* point of view in epistemology. As such, traditional Bayesian confirmation theorists who tend to assume that all confirmation judgments must *supervene* on some credence function (sometimes, perhaps a historical or counterfactual one) may not always be happy with my examples. As far as I can see, this is bad news for traditional Bayesian confirmation theory, since these examples — even the ones that cannot be given an internalist gloss — seem compelling to me. Besides, I think that the problem of old evidence has already showed us that this supervenience assumption implicit in traditional Bayesian confirmation theory is false. That can be seen with reference to my pregnancy test example by thinking about cases in which the agent already knows that the outcome of the test was positive. To my mind, this is *irrelevant* to whether E evidentially supports H . Intuitively, E supports H here *whether or not* E is already known to have occurred. It seems that this directs us toward an externalist notion of evidence, and I am perfectly happy with that. I am not suggesting that my theory won't apply to subjective evidential relations, just that its most interesting and compelling applications are to cases involving objective evidential relations (*e.g.*, those discussed by non-Bayesian statisticians).

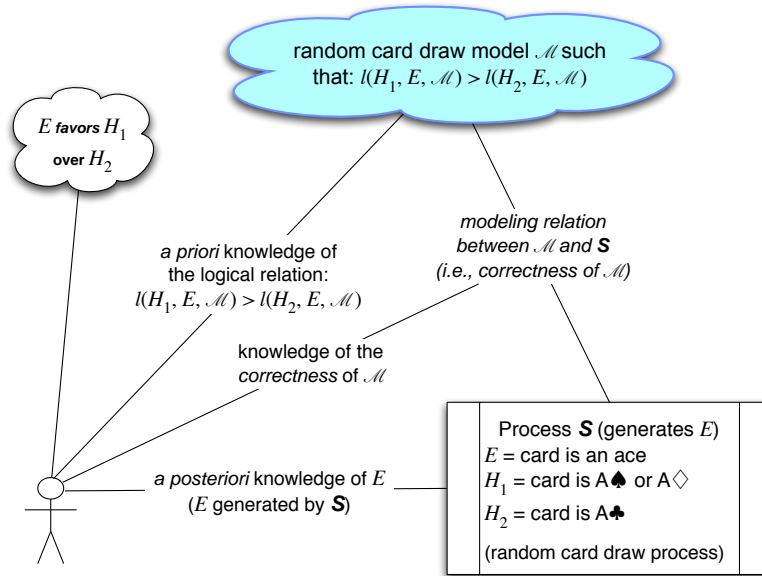


Figure 3: Comparative confirmation and favoring

that in such cases the agent knows (*ceteris paribus*) that E favors H_1 over H_2 . That is, the agent may infer in such cases that E constitutes better evidence for the truth of H_1 than for the truth of H_2 . I have intentionally chosen an example here in which there are other measures of confirmation as increase in firmness which disagree with l on this comparative claim. For instance, if we follow Milne (1996) and use the ratio measure $r(H, E, \mathcal{M}) = \log \left[\frac{\text{Pr}_{\mathcal{M}}(H|E)}{\text{Pr}_{\mathcal{M}}(H)} \right]$, then we get $r(H_1, E, \mathcal{M}) = r(H_2, E, \mathcal{M})$ in this example, which would *not* undergird the inference that E favors H_1 over H_2 . This sort of example reflects a long-standing controversy over alternative probabilistic accounts of comparative (or relational) confirmation (and support). I don't have the space here to expand on this controversy, but I have written extensively on it elsewhere (Fitelson 2006).

5 Conclusion

Carnap tried to provide an inductive-logical foundation for (epistemic) *probability*. I have explained what I think the shortcomings of his project were. Mainly, these involved problems with simultaneously satisfying three Carnapian desiderata for inductive logic, which I have called analyticity, logicity, and applicability. I then explained how one can overcome these difficulties by opting for an inductive-logical foundation for a *different* epistemic concept: *evidential support*. I briefly sketched my favored theory of inductive logic (in this sense), and I explained how it can simultaneously satisfy all three of our Carnapian

desiderata for inductive logic. Moreover, I argued that the resulting framework is widely and intuitively applicable to the interpretation of statistical evidence. I have provided only a broad sketch of how I think this new approach to inductive logic should work. I plan to produce a fuller treatment in a future monograph.

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