Conditionals

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Example Conditionals

- 1. If the Axiom of Choice is true, then every set can be well ordered.
- 2. You will probably get lung cancer if you smoke.
- If the syrup forms a soft ball when you drop it into cold water, then it is between 112 and 115 degrees Celsuis.
- 4. If kangaroos had no tails, they would topple over.
- 5. When I rule this land, you will be sorry.

 decision-making: to figure out what to do, you should consider, for each action you might choose, what would happen if you chose it.

controversial definition of expected utility:

$$EU(A) = \sum_{i} P(A \rightarrow O_{i})U(O_{i})$$

- science and philosophy of science: when deciding which theory to believe, you should consider, for each theory, what evidence you should expect if it is true.
- make-believe and imagination: what if you could talk to dolphins...

- **philosophy**: conditionals are used to formulate philosophically important concepts.
- B counterfactually depends on A iff:
 - If A had occurred, B would have occurred.
 - If A had not occurred, B would not have occurred.

- **philosophy**: conditionals are used to formulate philosophically important concepts.
- A is a *cause* of B iff both occurred and...
 - B counterfactually depends on A?
 - B counterfactually depends on something that counterfactually depends on A?
 - (More complicated conditions can be formulated in terms of causal graphs.)

- **philosophy**: conditionals are used to formulate philosophically important concepts.
- Dispositions
 - If X were in condition C, it would show manifestation M.
- Example: fragility
 - If this vase were dropped, it would break.

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- Being a law:
 - Say that S is a *stable set* iff, for every every *s* in S proposition *P* consistent with every *s* in *S*:
 - If *P* had been the case, *s* would still be the case.
 - S is a law iff it is a member of some non-maximal stable set.

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- S knows that P iff:
 - \circ P is true.
 - S believes that P.
 - If P had been true, S would have believed it.
 - If P had not been true, S wouldn't have believed it.

- **philosophy**: conditionals are used to formulate philosophically important concepts.
- S did A *freely* iff:
 - S did A on purpose, and
 - if S had wanted not to do A, then S would not have done A.

Indicative vs. Counterfactual

INDICATIVE: If Oswald didn't kill Kennedy, then someone else did.

COUNTERFACTUAL: If Oswald hadn't killed Kennedy, then someone else would have.

Indicative vs. Counterfactual

INDICATIVE: If Stephanie Kwolek didn't invent kevlar, then we can't use it in superconductors. COUNTERFACTUAL: If Stephanie Kwolek hadn't invented kevlar, then we wouldn't be able to use it in superconductors.

Indicative vs. Counterfactual

INDICATIVE: If Tupac is still alive, then every radio station in the country is playing his music. COUNTERFACTUAL: If Tupac was still alive, then every radio station in the country would be playing his music.

Features to Investigate

- **Truth conditions**: what does it take for a conditional to be true?
- Logic: which ways of reasoning with conditionals are valid?
- Pragmatics: what happens when you assert a conditional

Common Inferences

- Modus Ponens: $A \rightarrow B, A \vdash B$
- Pseudo Modus Ponens: $A \rightarrow B \vdash \neg A \lor B$
- Modus Tollens: $\vdash A \rightarrow B, \neg B \vdash \neg A$
- Conditional Proof: If $A \vdash B$, then $\vdash A \rightarrow B$
- **Deduction Theorem:** If A1, A2,..., An, $B \vdash C$, then A1, A2,..., An $\vdash B \rightarrow C$
- Import: $A \rightarrow (B \rightarrow C) \vdash (A \land B) \rightarrow C$
- **Export:** $(A \land B) \rightarrow C \vdash A \rightarrow (B \rightarrow C)$

Material Conditional



Bad Results About Probability

Suppose you roll a fair die. Consider the probability of:

- If you roll an even number, you roll a two.
- The material conditional "you roll an even number → you roll a two"?



The Strict Conditional



Exercises

- Show that (13-18) on the handout are valid if the conditional is the Material Conditional, but not if it's the Strict Conditional.
- Find counterexamples to these conditional analyses.
 - A is <u>true</u> iff, if there were an omniscient God, God would believe A.
 - X is <u>red</u> iff, if a normal perceiver looked at X under good conditions, it would look red.
 - I <u>believe</u> that A iff, were you to ask me whether P, I'd say yes.
 - A is <u>true according to a fiction</u> iff, if all of the sentences in the fiction were true, A would be true too.
- "If you eat that mushroom, then you will die." Is this conditional indicative, counterfactual, or neither?