## Knowledge Centered Epistemic Utility Theory

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## Outline

- 1. Prelude: Two Examples and an Overview of the Talk
- 2. Truth & The Old Lockeanism

- 3. Knowledge & A New Lockeanism
- ${\bf 4.\ Extras:\ Some\ Supplementary\ Slides\ {\it (hopefully\ useful\ in\ discussion)}}$

- **Miners** [34, 26]. You are standing in front of two mine shafts (*A* and *B*). Flood waters are approaching. You know that ten miners are in one of the shafts, but you don't know which (*e.g.*, their location was determined by the result of a fair coin toss). You have enough sand bags to block one of the shafts. If the miners are in *A*, then blocking *A* saves all 10 miners (and, hence, minimizes disutility, *i.e.*, # of dead miners). If the miners are in *B*, then blocking *B* minimizes disutility. If you block neither *A* nor *B*, the water will be divided, and only the lowest miner in the shaft will die.
  - **Claim.** *It is rationally permissible to block neither A nor B.*
- **Gibbard's Coin** [14, 30]. A fair coin has been tossed (and you have no information about how it landed). If it landed Heads (*H*), then believing *H* is the attitude which minimizes (epistemic) disutility (*viz.*, *inaccuracy*). If it landed Tails (*T*), then believing *T* is the attitude which minimizes inaccuracy. **Claim**. It is rationally permissible to believe neither *H* nor *T*.

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- Today's talk is about (i) formal, (ii) synchronic, (iii) epistemic (iv) coherence (v) requirements (of ideal rationality).
  - (i) *Formal* coherence is to be distinguished from other sorts of coherence discussed in contemporary epistemology (*e.g.*, in some empirical, truth/knowledge-conducive sense [1]).
    - Our notions of coherence will supervene on *logical* (and *formal probabilistic*) properties of judgment sets.
  - (ii) *Synchronic* coherence has to do with the coherence of a set of judgments held by an agent *S* at a single time *t*.
    - So, we'll not be discussing any diachronic [40] requirements
  - (iii) Epistemic coherence involves distinctively epistemic values (e.g., accuracy [19], evidential support [7], knowledge [Meno]).
    - This is to be distinguished from *pragmatic* coherence (e.g., immunity from dutch books [38], and the like [17]).
  - (iv) *Coherence* has to do with how a set of judgments "hangs together". CRs are *wide-scope* [3], global requirements.
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  - The Consistency Requirement for Belief. Agents should have *sets* of beliefs that are *logically consistent*.
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Extras

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- We assume that our agent takes exactly one of three qualitative attitudes (B, D, S) toward each member of a finite agenda  $\mathcal{A}$  of (classical, possible worlds) propositions.
- We do *not* assume that these qualitative judgments can be *reduced* to  $b(\cdot)$ . But, we will use  $b(\cdot)$  to derive a *rational coherence constraint* for qualitative judgment sets B (on  $\mathcal{A}$ ).
- This derivation requires both the agent's credence function b(·) and their *epistemic utility function* [18, 29, 31] u(·).
   Following Easwaran [11] & Dorst [9], we assume our agent cares *only* about whether their judgments are *accurate*.
- Specifically, our agent attaches some *positive* utility (r) with making an *accurate* judgment, and some *negative* utility (-w) with making an *inaccurate* judgment (where w > r > 0).

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- Because suspensions are neither accurate nor inaccurate (per se), our agent will attach zero epistemic utility to suspensions S(p), independently of the truth-value of p.
- Thus, we have the following piecewise definition of  $u(\cdot, w)$ .

$$u(B(p), w) \stackrel{\text{def}}{=} \begin{cases} -w & \text{if } p \text{ is false at } w \\ r & \text{if } p \text{ is true at } w \end{cases}$$

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- To do so, we'll also need a *decision-theoretic principle*.
- As we saw, applications of EUT to grounding probabilism as a (synchronic) requirement for  $b(\cdot)$  typically appeal to a *non-dominance* (in epistemic utility) principle [20, 37, 35].
- But, some authors apply an expected epistemic utility maximization (or expected inaccuracy minimization) principle to derive rational requirements [28, 16, 12, 33].

$$EEU(\mathbf{B}, b) \cong \sum_{p=2}^{\infty} \sum_{w \in W} b(w) \cdot u(\mathbf{B}(p), w)$$

where  $\mathbf{B}(p)$  is the agent's attitude toward p, and  $W \cong \bigcup \mathcal{A}$ .

 We also assume "act-state independence": B(p) and p are b-independent [15, 5, 4, 27]. See Extras for discussion.

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• The consequences of **Coherence** are rather simple and intuitive. It is straightforward to prove the following result.

**Theorem** ([11, 9]). An agent with credence function  $b(\cdot)$  and qualitative judgment set **B** over agenda  $\mathcal{A}$  satisfies **Coherence** *if and only if* for all  $p \in \mathcal{A}$ 

$$B(p) \in \mathbf{B} \text{ iff } b(p) > \frac{w}{r+w},$$

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$$S(p) \in \mathbf{B} \text{ iff } b(p) \in \left[\frac{r}{r+w}, \frac{w}{r+w}\right].$$

- In other words, **Coherence** *entails Lockean representability*, where the Lockean thresholds are determined by the way the agent (relatively) values accuracy *vs.* inaccuracy.
- This provides an elegant, EUT-based explanation of why Lockean representability is a rational requirement for agents with *both* credences *and* qualitative attitudes.

$$\begin{split} B(p) &\in \mathbf{B} \text{ iff } b(p) > \frac{w}{\mathsf{r} + \mathsf{w}}, \\ D(p) &\in \mathbf{B} \text{ iff } b(p) < \frac{\mathsf{r}}{\mathsf{r} + \mathsf{w}}, \\ S(p) &\in \mathbf{B} \text{ iff } b(p) \in \left[\frac{\mathsf{r}}{\mathsf{r} + \mathsf{w}}, \frac{w}{\mathsf{r} + \mathsf{w}}\right]. \end{split}$$

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- This provides an elegant, EUT-based explanation of why Lockean representability is a rational requirement for agents with *both* credences *and* qualitative attitudes.
- As Dorst [9] puts it: *Lockeans maximize expected accuracy*.

## • In the *Meno* (97e-98a), Socrates says:

For true opinions, as long as they remain, are a fine thing and all they do is good, but they are not willing to remain long, and they escape from a man's mind, so that they are not worth much until one ties them down ... That is why knowledge is prized higher than correct opinion, and knowledge differs from correct opinion in being tied down...

- Our epistemic utility function (for belief) only assigned positive value to *correctness*. What about *knowledge*?
- Nothing in our (teleological) framework for epistemic utility theory rules out attaching (additional) value to *knowledge*, over and above the value we place on correctness/accuracy.
- There are various ways one might refine/alter our naïve (accuracy centered) epistemic utility function, so as to take account of this Meno-style *value of knowledge*.
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K(p)	a	x
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- When we represent things at this level of generality, we realize there are (at least) two key *choice points* here.
  - (1) Are knowledge and truth *both* positively valuable (or is knowledge *the only* state that has positive value)? That is: should we have *both* x > 0 *and* y > 0, or *just* x > 0?
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- These choices especially (1) will impact the kinds of "Lockean Theses" that fall out of the models (via MEEU).

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- The simplest models would be ones in which *only* knowledge has positive value (*i.e.*, greater than suspension).
- Such models which answer (1) in the negative will all yield constraints of the following (general) form:

- Models which answer (1) in the *affirmative*, are far more complex, and can be compatible with b(K(p)) being *arbitrarily low*. We don't have a full characterization of those models, but we have some special cases worked out.
- Let's focus on the simplest models (and Lotteries). First, a review of *accuracy*-centered models (and Lotteries).

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Extras

 By way of summary, it is useful to think about the analogy between the norms we've been discussing, and principles of rational choice theory: The Decision-Theoretic Analogy.

Epistemic Principle	Analogous Decision-Theoretic Principle
Alethic Ideal	(AMU) Do $\phi$ only if $\phi$ maximizes utility in the <i>actual</i> world.
Consistency	(PMU) Do $\phi$ only if $\phi$ maximizes $u$ in <i>some possible</i> world.
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- Like the **Alethic Ideal**, (AMU) is *not* a *requirement of rationality*; and, like **Consistency**, (PMU) isn't a rational requirement either (this was the lesson of **Miners** [34, 26]).
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There does *not* exist an alternative belief set **B**' such that:

- (i)  $(\forall w)[u(B', w) \le u(B, w)]$ , and
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- Sharon Ryan [39] gives an argument *for* (CB) as a rational requirement, which makes use of these three premises.
  - The Closure of Rational Belief Principle (CRBP). If S rationally believes p at t and S knows (at t) that p entails q, then it would be rational for S to believe q at t.
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$w_1$	F	T	_	+	-	-	×	×	×	×
$w_2$	T	F	×	×	×	×	_	-	_	+

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Extras

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