

### Some Final Thoughts (for now) on Skyrms

- Administrative: in the next week or two, you should begin thinking about your topics for the first short paper (see me)
- Re-cap of Worked Probability Example from Last Time
- Re-cap of Skyrms's Account of Inductive Strength
  - Understanding Skyrms' Rejection of " $\sim q \& p$ " Account
  - Virtues of Skyrms' " $\sim q$  given  $p$ " Account
  - Vices of Skyrms' " $\sim q$  given  $p$ " Account
- Moving Beyond Skyrms' Account of Inductive Strength
- Segue Into Bayesian Confirmation (Skyrms Chapter 8)
- Next Time: Salmon & Earman on Confirmation (Reader)

### Reasoning About Probabilities: A Worked Example

- Let  $q$  = 'a card drawn at random from a standard deck is *not* a face card', and  $p$  = 'the card is a spade.' We assume  $\Omega$  is the usual reference class for standard (well-shuffled) decks of playing cards.
- The four basic probabilities regarding  $p$  and  $q$  are:
  - $\Pr(p \& \sim q) = \alpha = \frac{\# \text{ of face spades}}{\text{total \# of cards}} = \frac{3}{52}$
  - $\Pr(p \& q) = \beta = \frac{\# \text{ of non-face spades}}{\text{total \# of cards}} = \frac{10}{52}$
  - $\Pr(\sim p \& q) = \gamma = \frac{\# \text{ of non-face non-spades}}{\text{total \# of cards}} = \frac{30}{52}$
  - $\Pr(\sim p \& \sim q) = \delta = \frac{\# \text{ of face non-spades}}{\text{total \# of cards}} = \frac{9}{52}$

$\Pr(p) = \alpha + \beta = \frac{13}{52}$	$\Pr(q) = \beta + \gamma = \frac{40}{52} = \frac{10}{13}$
$\Pr(p   q) = \frac{\Pr(p \& q)}{\Pr(q)} = \frac{10/52}{10/13} = \frac{13}{52}$	$\Pr(q   p) = \frac{\Pr(p \& q)}{\Pr(p)} = \frac{10/52}{13/52} = \frac{10}{13}$
$\Pr(p   q) = \Pr(p), \therefore p \perp q$	$\Pr(q   p) = \Pr(q), \therefore q \perp p$
$\Pr(q   p)$ is <i>high</i> ( $\approx 0.77$ ). But, is $\frac{p}{\therefore q}$ (intuitively) a <i>strong argument</i> ?	

### Re-cap of Skyrms on Inductive Strength I

- Skyrms (pp. 20–21) gives two examples, *both* of which show that:

$$\Pr(\sim q \& \mathbf{P}) \text{ is low} \not\Rightarrow \frac{\mathbf{P}}{\therefore q} \text{ is inductively strong.}$$

- In Skyrms' first example (p. 20),  $\sim q \& \mathbf{P}$  is improbable *merely because*  $\mathbf{P}$  — by itself — is improbable. Skyrms correctly points out that  $\mathbf{P}$  *need not* be 'evidentially relevant' to  $q$  in such cases.
- **Question:** Does  $\mathbf{P} \perp q$  hold in Skyrms' first example? Use your answer to this question to say something about whether  $\mathbf{P}$  is 'evidentially relevant' to  $q$  in Skyrms' *particular* example on page 20. **Hint:** "If  $p \models q$ , then  $\Pr(p) \leq \Pr(q)$ " is *crucial* here (*why?*).
- **New Paper Topic:** Give a compelling demonstration that:

$$\Pr(\sim q \& \mathbf{P}) \text{ is low} \not\Rightarrow \frac{\mathbf{P}}{\therefore q} \text{ is inductively strong.}$$

### Re-cap of Skyrms on Inductive Strength II

- Here is Skyrms' second counterexample (page 21) to the claim that:

$$\Pr(\sim q \& \mathbf{P}) \text{ is low} \implies \frac{\mathbf{P}}{\therefore q} \text{ is inductively strong}$$

(p) There is a man in Celevland who is 1999.99 y.o. and in good health.

(q)  $\therefore$  No man will live to be 2000 years old.

- Assuming the reference class  $\Omega$  consists of the propositions in our store of background knowledge concerning the life span of human beings, Skyrms argues (plausibly) that the following probabilistic facts obtain:
  - $\Pr(q) = \Pr(q | \Omega)$  is *high*. Therefore,  $\Pr(\sim q) = 1 - \Pr(q)$  is *low*.
  - Hence,  $\Pr(\sim q \& p)$  is *also* low [If  $p \models q$ , then  $\Pr(p) \leq \Pr(q)$ !].
  - But, this argument is **NOT** inductively strong, since  $p$  is evidence *against*  $q$ . Thus,  $\Pr(\sim q \& \mathbf{P})$  is low  $\not\Rightarrow \frac{\mathbf{P}}{\therefore q}$  is inductively strong. *QED.*
- **Question:** Does Skyrms' account (*necessarily*) give the *right* answer?

### Rethinking Skyrms' Account of Inductive Strength I

- First, let's state Skyrms' definition more precisely:

– An argument  $\frac{\mathbf{P}}{\therefore q}$  is inductively strong iff  $\Pr(\sim q | \mathbf{P})$  is low.

- I find the following *equivalent* definition more perspicuous:

– An argument  $\frac{\mathbf{P}}{\therefore q}$  is inductively strong iff  $\Pr(q | \mathbf{P})$  is high.

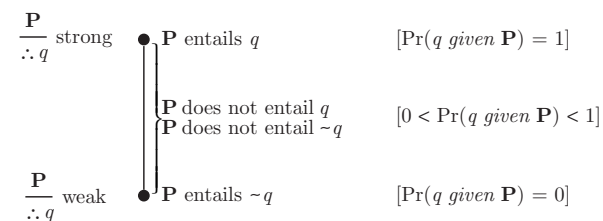
- It should be clear why *neither* of these is equivalent to “ $\Pr(\sim q \& \mathbf{P})$  is low.” This is clear from the definition of conditional probability:

$$\Pr(\sim q | \mathbf{P}) = \frac{\Pr(\sim q \& \mathbf{P})}{\Pr(\mathbf{P})} \neq \Pr(\sim q \& \mathbf{P}) \quad [\text{unless } \Pr(\mathbf{P}) = 1]$$

- The “ $\sim q \& \mathbf{P}$  is improbable” proposal does *not* properly generalize the *deductive* notion of support. This is surprising, since “ $\sim q \& \mathbf{P}$  is *improbable*” is the natural inductive weakening of “ $\sim q \& \mathbf{P}$  is *impossible*”. On this score, Skyrms' account is superior ...

### Rethinking Skyrms' Account of Inductive Strength II

- On page 22, Skyrms gives (something like) the following diagram:



- We seek a measure  $s(q, \mathbf{P})$  of the strength of  $\frac{\mathbf{P}}{\therefore q}$  such that (*at least*):
  1. If  $\mathbf{P} \models q$ , then  $s(q, \mathbf{P})$  is *maximal*.
  2. If  $\mathbf{P} \not\models q$  and  $\mathbf{P} \not\models \sim q$ , then  $s(q, \mathbf{P})$  is *intermediate*.
  3. If  $\mathbf{P} \models \sim q$ , then  $s(q, \mathbf{P})$  is *minimal*.
- Skyrms' measure  $s(q, \mathbf{P}) = \Pr(q | \mathbf{P}) = 1 - \Pr(\sim q | \mathbf{P})$  satisfies 1–3. Does “ $1 - \Pr(\sim q \& \mathbf{P})$ ”? What about the “*relevance*” of  $\mathbf{P}$  to  $q$ ?

### Rethinking Skyrms' Account of Inductive Strength III

- Measures satisfying properties 1–3 on the previous slide have the virtue of capturing *deductive* relations as *limiting cases*.
- In this sense,  $\Pr(q | \mathbf{P})$  is *more* sensitive than  $\Pr(\sim q \& \mathbf{P})$  to ‘evidential relations’ (at least, *deductive* ones) between  $\mathbf{P}$  and  $q$ .
- But, what about the relation of *probabilistic relevance* (*i.e.*,  $\not\perp$ )?
- As we have seen, even  $\Pr(q | \mathbf{P})$  does *not* adequately gauge the *probabilistic* (*a.k.a.*, *stochastic*) relevance relation between  $\mathbf{P}$  and  $q$ .
- Perhaps we should think of Skyrms' proposed measure of the degree to which  $p$  supports  $q$  —  $\Pr(q | p)$  — as *merely* a measure of the “degree to which  $p$  *deductively* supports  $q$ ”. This makes sense, given the way we define/interpret conditional probability, no?
- **Another Example:**  $p$  = “Fred Fox has been (properly) taking birth control pills for 2 years,”  $q$  = “Fred Fox is not pregnant.” Is the argument from  $p$  to  $q$  a strong one (intuitively)? Is  $\Pr(\sim q | p)$  low?

### ‘Relevance’ in the *Deductive* Support Relation

- Skyrms' complaint about the “ $\sim q \& \mathbf{P}$  is improbable” account of inductive strength is (roughly) that  $\sim q \& \mathbf{P}$  can be improbable *even if* (intuitively)  $\mathbf{P}$  has “*nothing to do with*”  $q$ .
- Some philosophers of logic have had similar complaints about the “ $\sim q \& \mathbf{P}$  is *impossible*” account of (classical) *deductive* support.
- Such ‘relevant’ logicians point out the (intuitive) “irrelevance” of the premises and conclusions in the following *valid* arguments:

$$\frac{p \& \sim p}{\therefore q} \qquad \frac{p}{\therefore q \vee \sim q}$$

- How does Skyrms' measure of strength judge these arguments?
- Perhaps we want *more* from a measure of *inductive* strength than *merely* a gauge “partial entailment” ... perhaps we also want sensitivity to *other* (*inductive!*) kinds of *evidential relevance* ...

### Relevance Measures of Inductive Support

- We seek a measure  $s(q, p)$  of the degree to which  $p$  supports  $q$  such that:
  1.  $s$  captures the *deductive* relations as *limiting cases* (previous slide),
  2.  $s$  is *also* sensitive to *probabilistic relevance*.
- What (2) says is that we want a measure  $s(q, p)$  which is *positive* if  $p$  *raises* the probability of  $q$ , *negative* if  $p$  *lowers* the probability of  $q$ , and *zero* if  $p \perp q$ . That is, we want  $s(q, p)$  to be a *relevance measure*:

$$s(q, p) \begin{cases} > 0 & \text{if } \Pr(q | p) > \Pr(q), \\ < 0 & \text{if } \Pr(q | p) < \Pr(q), \\ = 0 & \text{if } \Pr(q | p) = \Pr(q) \quad [\text{i.e., if } p \perp q]. \end{cases}$$

- We know that Skyrms' measure  $c(q, p) = \Pr(q | p)$  satisfies (1) but *not* (2).
- **Exercises:** Show that  $d(q, p) = \Pr(q | p) - \Pr(q)$  satisfies (2) but *not* (1). Show that  $l(q, p) = \frac{\Pr(p|q) - \Pr(p|\neg q)}{\Pr(p|q) + \Pr(p|\neg q)}$  satisfies *both* (1) *and* (2)! How does  $l(q, p)$  judge the “irrelevant” deductive arguments on the previous slide?

### Skyrms' Chapter 8: Applications (*segue* to confirmation)

- In chapter 8, Skyrms starts talking about applications of inductive logic to philosophy of science (basically, to “confirmation”).
- How does Skyrms suggest (page 152) we should capture Popper's relation of “corroboration” — using inductive probability?
- How does Skyrms unpack the comparative relation: “ $p$  is better evidence for  $q$  than  $r$  is for  $s$ ” in chapter 8?
- Are these concepts (*i.e.*, “corroborative evidence” and “better evidence”) already implicit in his definition of inductive strength?
- If not, might this be a *weakness* of his account of inductive strength? Can we give problematic *examples* here (Fred Fox)?
- Can you think of alternative ways to define inductive strength that might overcome these weaknesses (*i.e.*, that might capture all of these notions under the single umbrella of “inductive strength”)?